

COSMOLOGY: ORIGIN & STRUCTURES

ON COSMOLOGICAL VELOCITY FIELDS

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Vincent Bouillot



AGENDA

I. Introduction

II. Large-scale cosmological velocity fields

III. Statistical interpretation of high velocity cosmic flows

IV. Large-scale asymmetry: origin of high velocity cosmic flows

V. Spatial distribution of high velocity cosmic flows

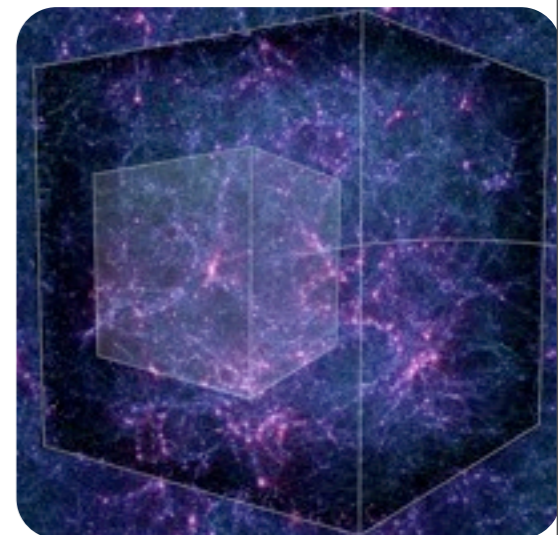
VI. Bullet Cluster: A challenge to standard cosmology?

VII. Conclusion



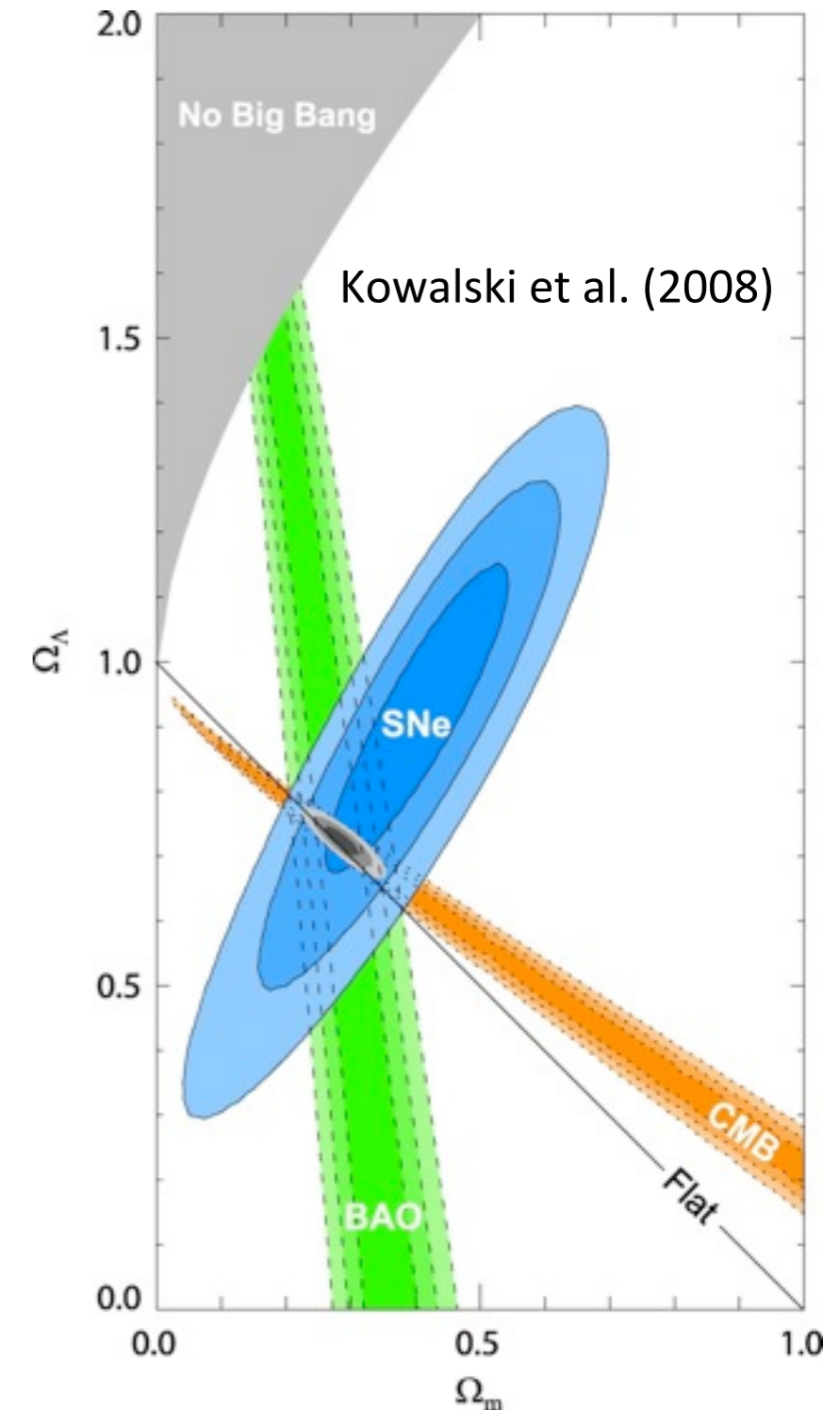
I. INTRODUCTION

- 1) Discovery of a Dark Sector
- 2) Dark Energy - Structure formation
- 3) N-body simulations
- 4) Cosmological velocity fields



DISCOVERY OF A DARK SECTOR

- ❖ The Universe is a dynamical physical system.
- ❖ Cosmic expansion is accelerated:
 - ◆ This acceleration is driven by an unknown form of energy.
 - ◆ What is the amount of Dark Energy?
- ❖ Supernovae Ia, Cosmic Microwave Background, Baryonic Acoustic Oscillations.





DARK ENERGY - STRUCTURE FORMATION

- ❖ What is the nature of Dark Energy?
 - ◆ Numerous concurrent Dark Energy models
- ❖ How can we distinguish various Dark Energy models?
- ❖ Solution: use of structure formation and gravitational non-linear clustering.
 - ◆ What can we learn on Dark Energy from structure formation?
 - ◆ Conversely, what is the impact of Dark Energy on structure formation?



STRUCTURE FORMATION

- ❖ Structure formation and gravitational clustering are non-linear processes.
- ❖ No analytic theories to fully describe the gravitational collapse from a linear to a non-linear phase, which is very important to understand structure formation:
 - ◆ Unavoidable use of the numerical tool.
- ❖ How should we proceed to perform numerical simulations of structure formation in Dark Energy models?
 - ◆ N-body simulations to follow gravitational clustering in realistic (i.e. in agreement with SNIa, CMB...) cosmological models.



N-BODY SIMULATIONS

- ❖ «Not too high» number of bodies: the main difficult part is the resolution of the Vlasov-Poisson equations.
- ❖ The DEUS consortium:
 - ◆ An highly scalable application called AMADEUS encompassing the whole simulation chain.
 - ▶ Initial conditions: realistic models.
 - ▶ Gravity solver (Vlasov-Poisson solver) - RAMSES-DEUS.
 - ▶ Post-processing (Slicing, Friends-of-Friends structure detection, filing of generated data...).



N-BODY SIMULATIONS

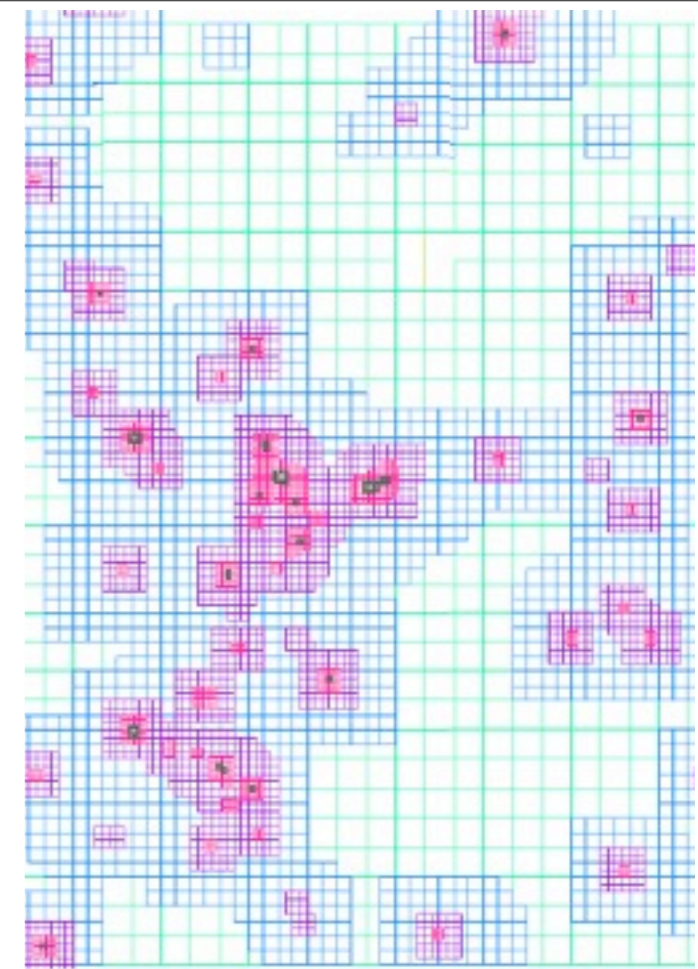
❖ The PM method in a nutshell:

1. Compute the mass density ρ on the **mesh** using an interpolation scheme from the position of **particles**.
2. Compute the potential ϕ on the **mesh** using the field equation.
3. Compute the acceleration on the **mesh**.
4. Compute each **particle** acceleration using the inverse interpolation scheme used in step 1.
5. Update each **particle** velocity and position - check energy conservation equation - modify the time-step.

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N-BODY SIMULATIONS

- ❖ Set of 31 cosmological simulations covering a large range of science topics (scales and cosmological models):

Boxlength (h^{-1} Mpc)	Resolution (h^{-1} kpc)	Mass resol. ($h^{-1} M_{\odot}$)	Number of particles	Initial redshift	Cosmological model	Computer (# of cores)
162	2.5	$2 \cdot 10^9$	512^3	90	Λ , SU, RP	Titane (64)
162	2.5	$2.5 \cdot 10^8$	1024^3	130	Λ , SU, RP	BlueGene/P (4096)
648	20	$1.5 \cdot 10^{11}$	512^3	55	Λ , SU, RP	-
648	10	$1.7 \cdot 10^{10}$	1024^3	90	Λ , SU, RP	BlueGene/P (4096)
648	5	$2 \cdot 10^9$	2048^3	90	Λ , SU, RP	BlueGene/P (32768)
1296	40	10^{12}	512^3	40	Λ , SU, RP	-
2592	40	10^{12}	1024^3	55	Λ , SU, RP	BlueGene/P (4096)
2592	20	$1.5 \cdot 10^{11}$	2048^3	55	Λ , RP	BlueGene/P (24576)
5184	40	10^{12}	2048^3	40	Λ , RP	BlueGene/P (24576)
10368	40	10^{12}	4096^3	100	Λ , RP, w	Curie Thin (9504)
21000	40	10^{12}	8192^3	100	Λ , RP, w	Curie Thin (76032)

N-BODY SIMULATIONS

❖ DEUS cosmological models:

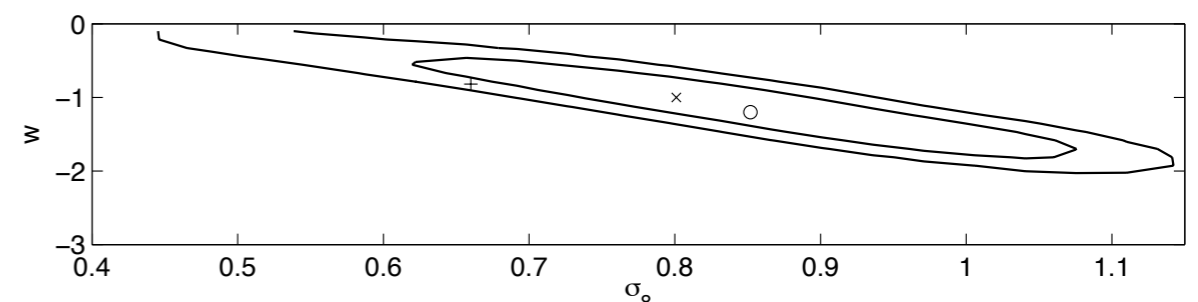
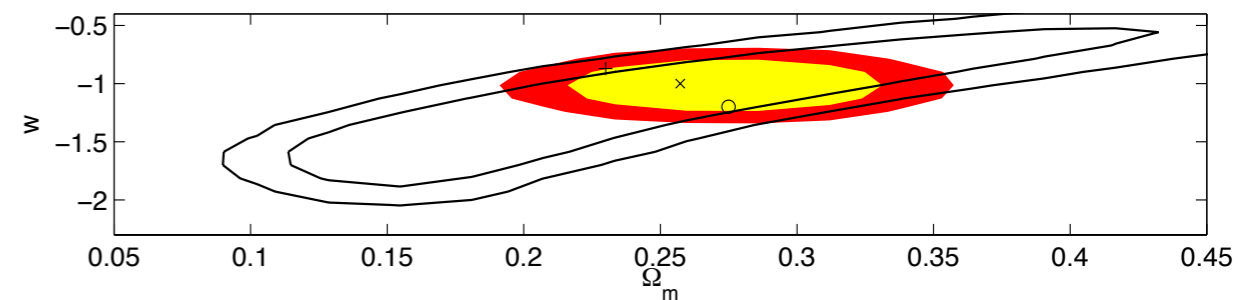
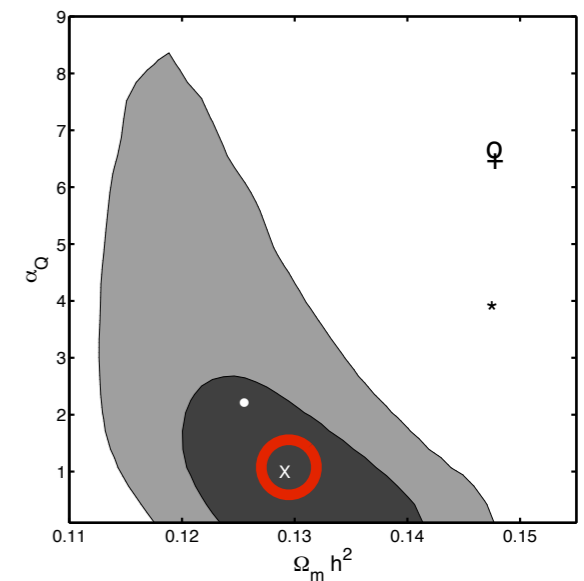
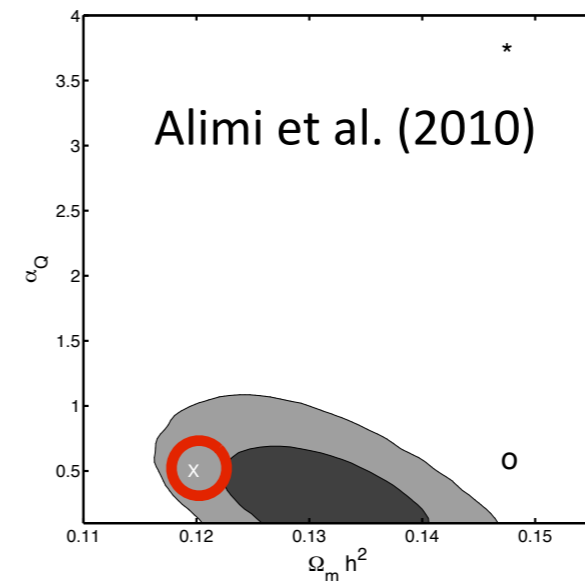
- ◆ Standard Λ CDM model.
- ◆ Quintessence models:

▶ Find the potential parameters:

- Ratra-Peebles: $V_{RP}(\varphi) = \frac{\lambda^{4+\alpha_Q}}{\varphi^{\alpha_Q}}$
- Supergravity: $V_{SU}(\varphi) = \frac{\lambda^{4+\alpha_Q}}{\varphi^{\alpha_Q}} e^{\frac{\kappa^2}{2}\varphi^2}$

◆ Phantom model:

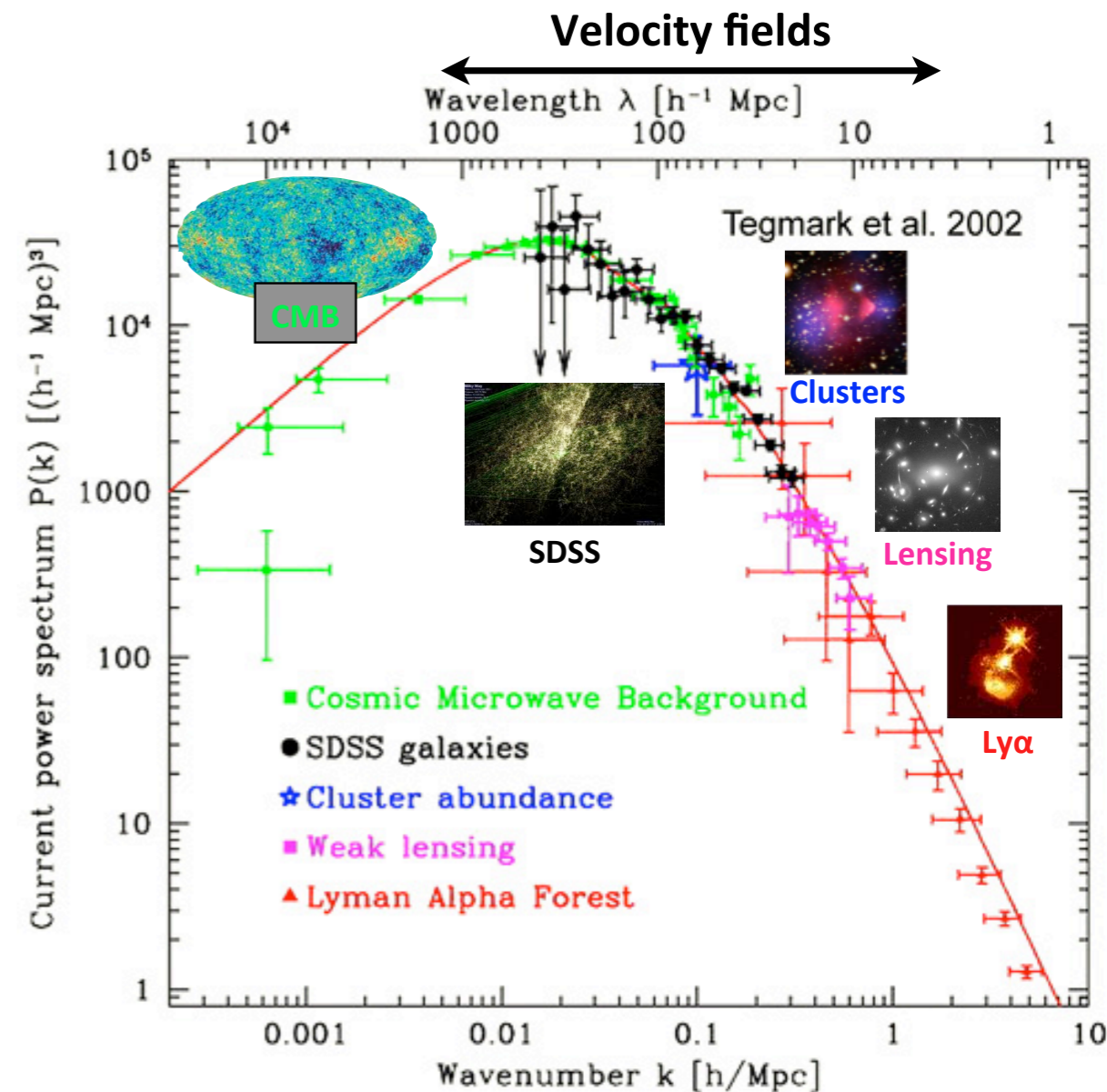
▶ Find the equation of state: w



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COSMOLOGICAL VELOCITY FIELDS

- ❖ Cosmological velocity fields:
 - ◆ Probe from small to large scales.
 - ◆ Sensitive to the total mass (not only the luminous baryons).
 - ◆ More sensitive to large scales than density fields.



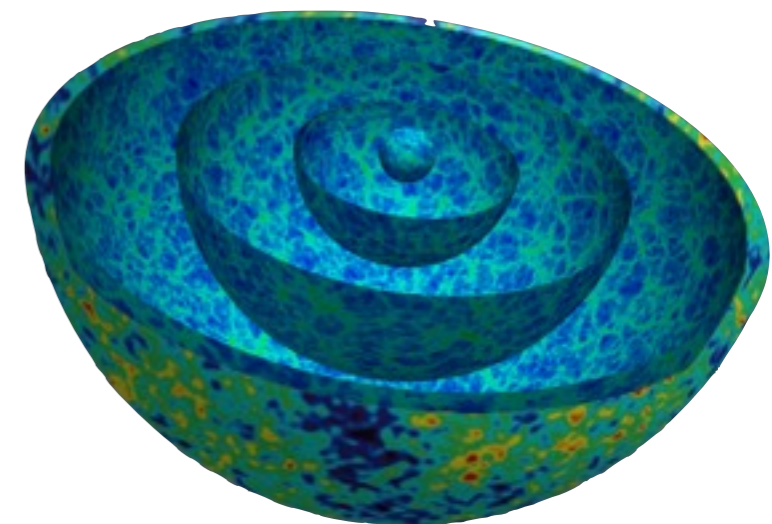
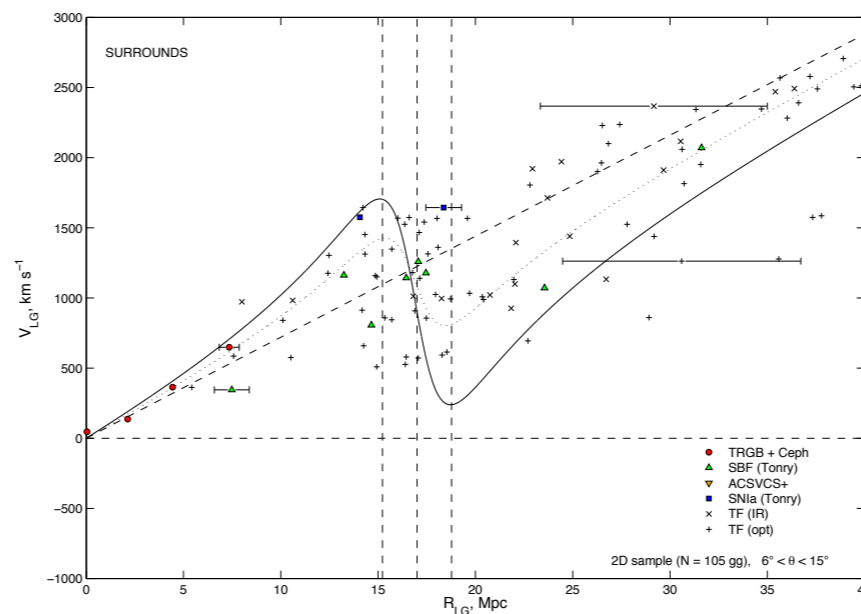
COSMOLOGICAL VELOCITY FIELDS

- ❖ Cosmological velocity fields:
 - ◆ Small scales: 1E0657-56 (Bullet cluster)
 - ◆ Intermediate scales: Virgocentric infall
 - ◆ Large scales: Bulk (spherically averaged) cosmic motion

Markevitch et al. (2002)



Karachentsev, Nasonova (2010)



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COSMOLOGICAL VELOCITY FIELDS

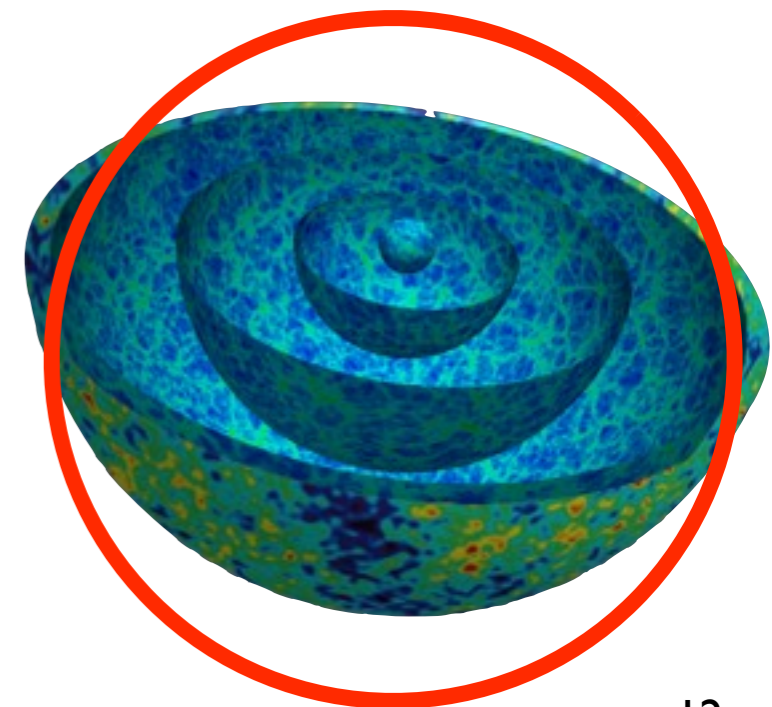
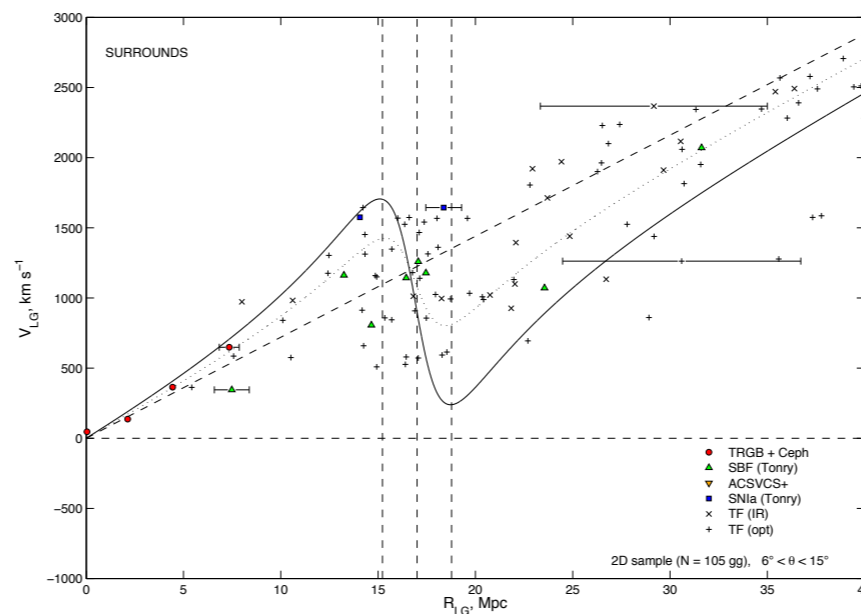
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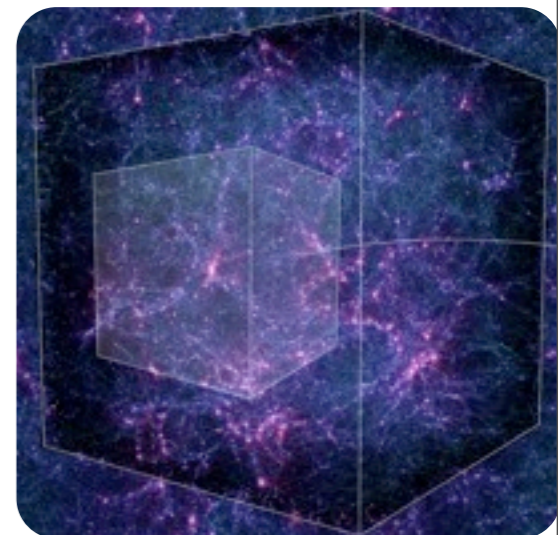


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VI. BULLET CLUSTER: A CHALLENGE TO STANDARD COSMOLOGY

- 1) Bullet clusters
- 2) Occurrence of bullets
- 3) Probability of bullets



BULLET CLUSTERS

- ❖ 1E0657-56 (BC) is the most famous bullet system:
 - ◆ Main cluster mass $10^{15} h^{-1} M_{\odot}$.
 - ◆ Ratio 10:1 at $z=0.296$.
 - ◆ The gas of the main cluster is ripped off the gravitational potential!
 - ◆ Velocity of the shock front is 4700 km/s.
 - ◆ Doesn't mean the dark matter velocity is so high.



BULLET CLUSTERS

❖ Other bullet systems:

- ◆ El Gordo (ACT-CL J0102-4915)
(mass ratio 2:1 $z=0.87$)



- ◆ MACS J0025.4-1222
(mass ratio 1:1 $z=0.586$)

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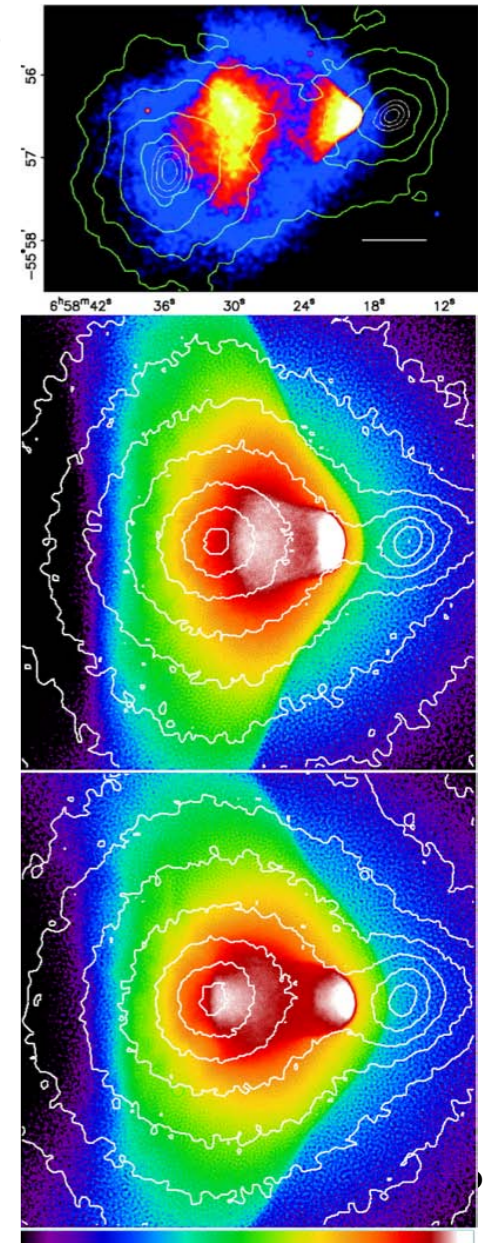
Imprints of Dark Energy on structure formation

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BULLET CLUSTERS

- ❖ How such galaxy cluster pairs form?
 - ◆ Mastropietro & Burkert (2008) pave the initial parameters space to understand how the gas of the main halo can be ripped of the potential (3D hydro simulation)
 - ◆ Initial conditions:
 - ▶ Initial redshift: $z=0.486$.
 - ▶ Mass ratios: 6:1 better than 10:1.
 - ▶ Initial relative (pairwise) velocities: 3000 km/s.
 - ◆ Careful: non-cosmological simulations.



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Imprints of Dark Energy on structure formation

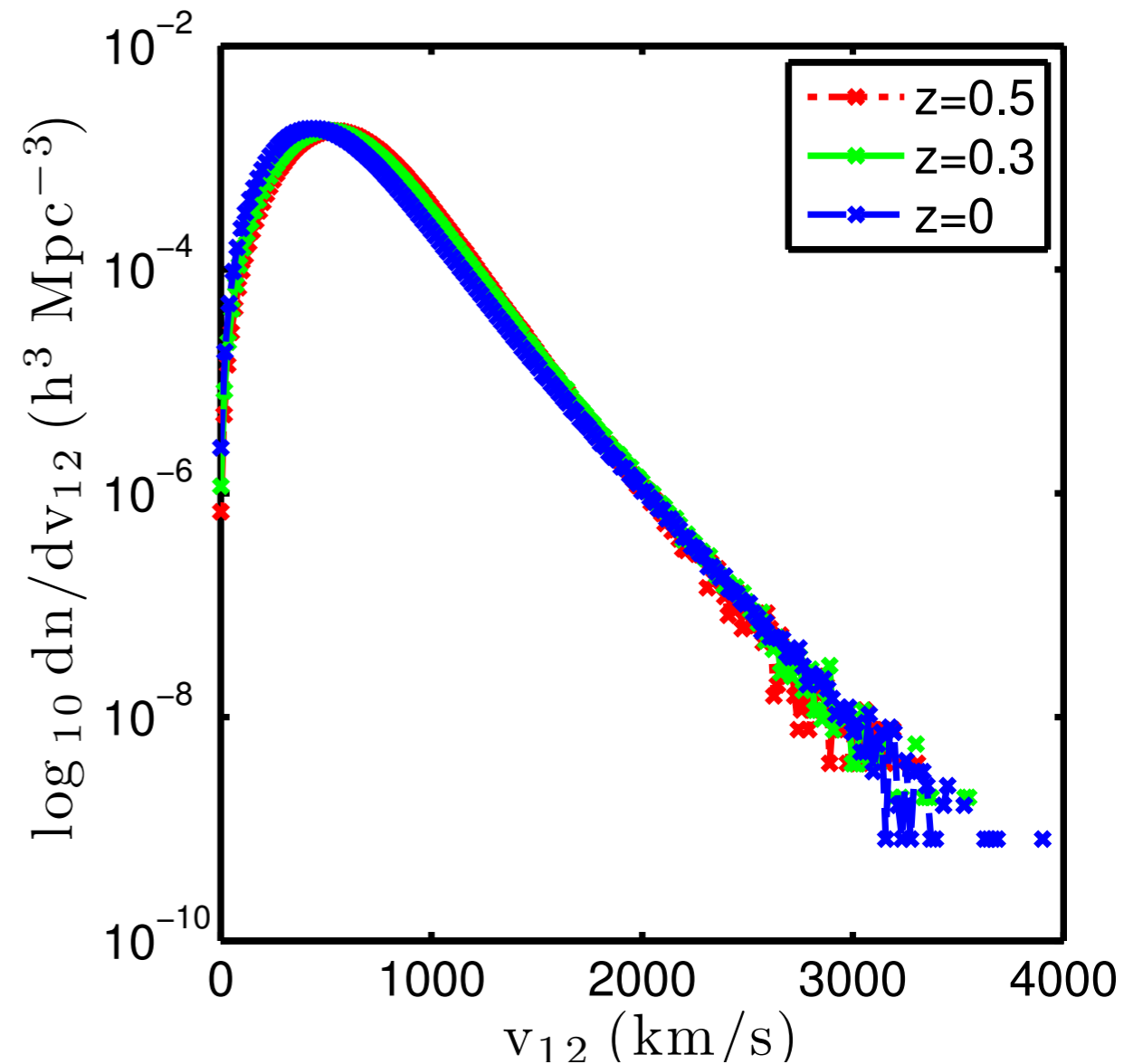


OCCURENCE OF BULLETS

- ❖ Is this a problem for the standard picture of cosmology?
- ❖ Such an event can rule out an entire cosmological model!
- ❖ Use very large numerical simulations to look for the initial conditions of Mastropietro & Burkert (2008).
 - ◆ DEUS: Full Universe Run is the perfect simulation:
 - ▶ High mass resolution.
 - ▶ Large volume to get extreme events and high halo abundance.

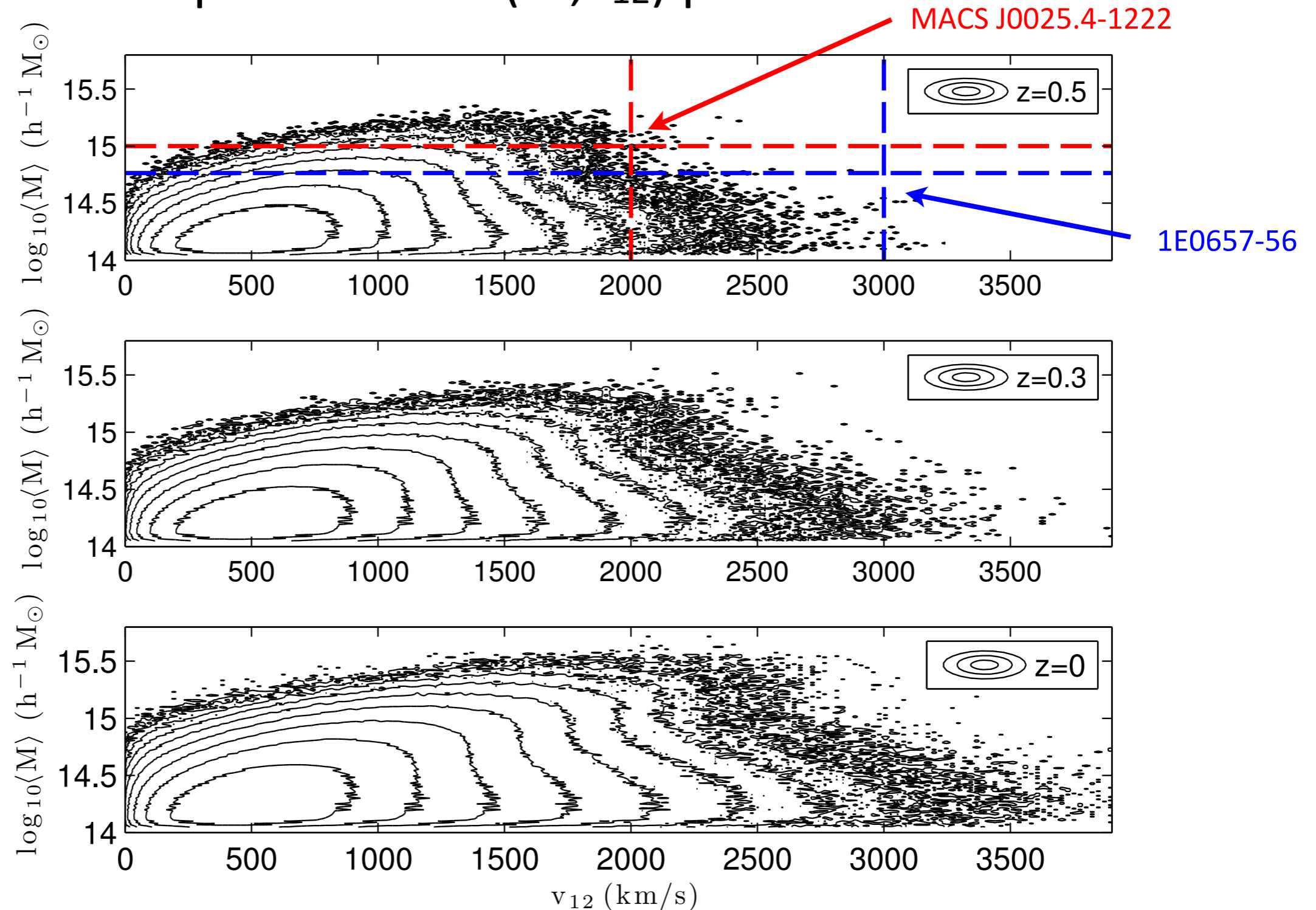
OCCURENCE OF BULLETS

- ❖ Distribution of v_{12} to know if some objects may have the good initial velocity:
 - ◆ Large pairs velocity are definitely there.
 - ◆ But, the BC initial conditions require a given average mass.
- ❖ Distribution in (M, v_{12}) plane to know if some objects may match the good initial condition.



OCCURENCE OF BULLETS

❖ Redshift dependence of (M, v_{12}) plane:

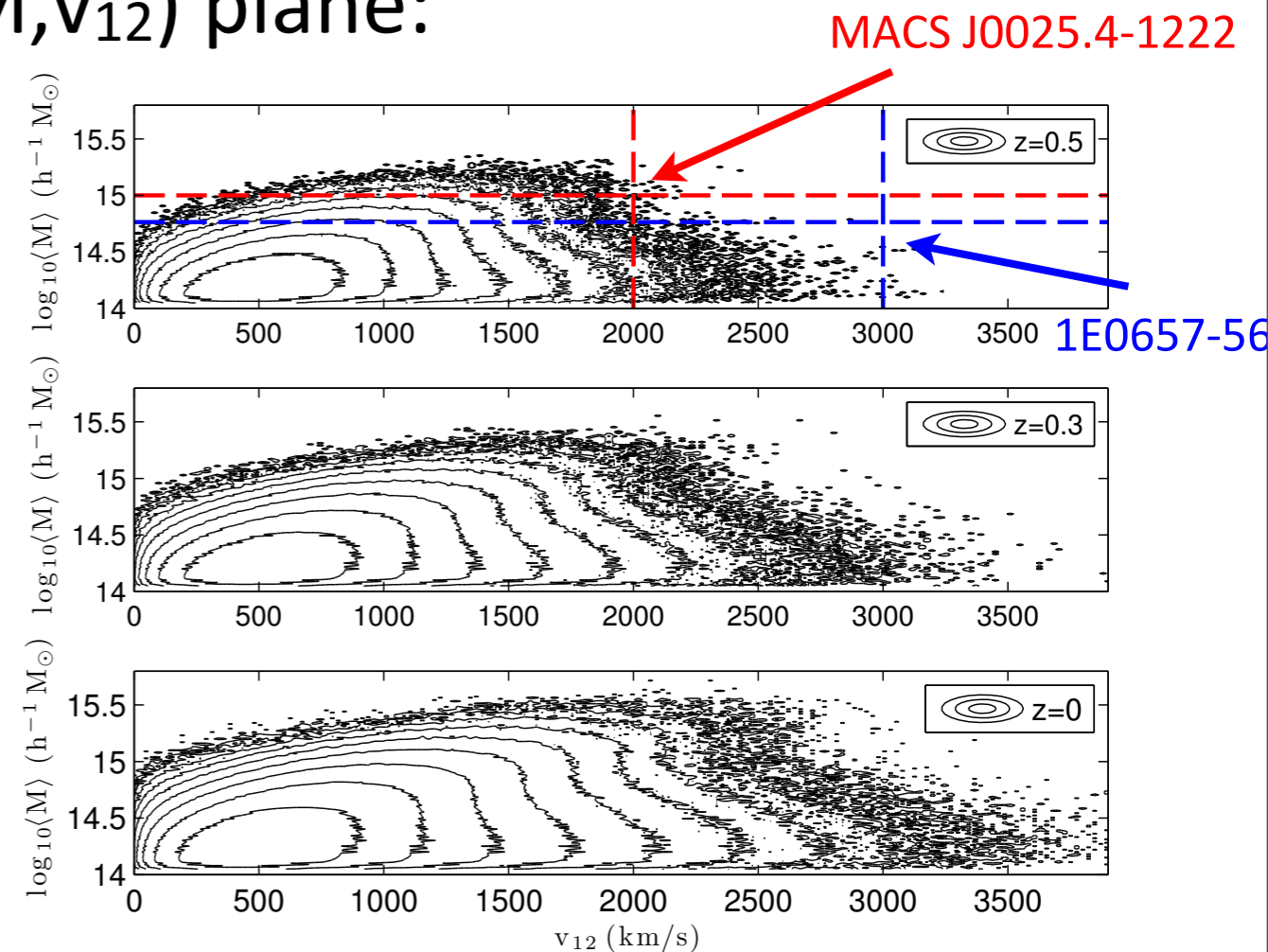


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OCCURENCE OF BULLETS

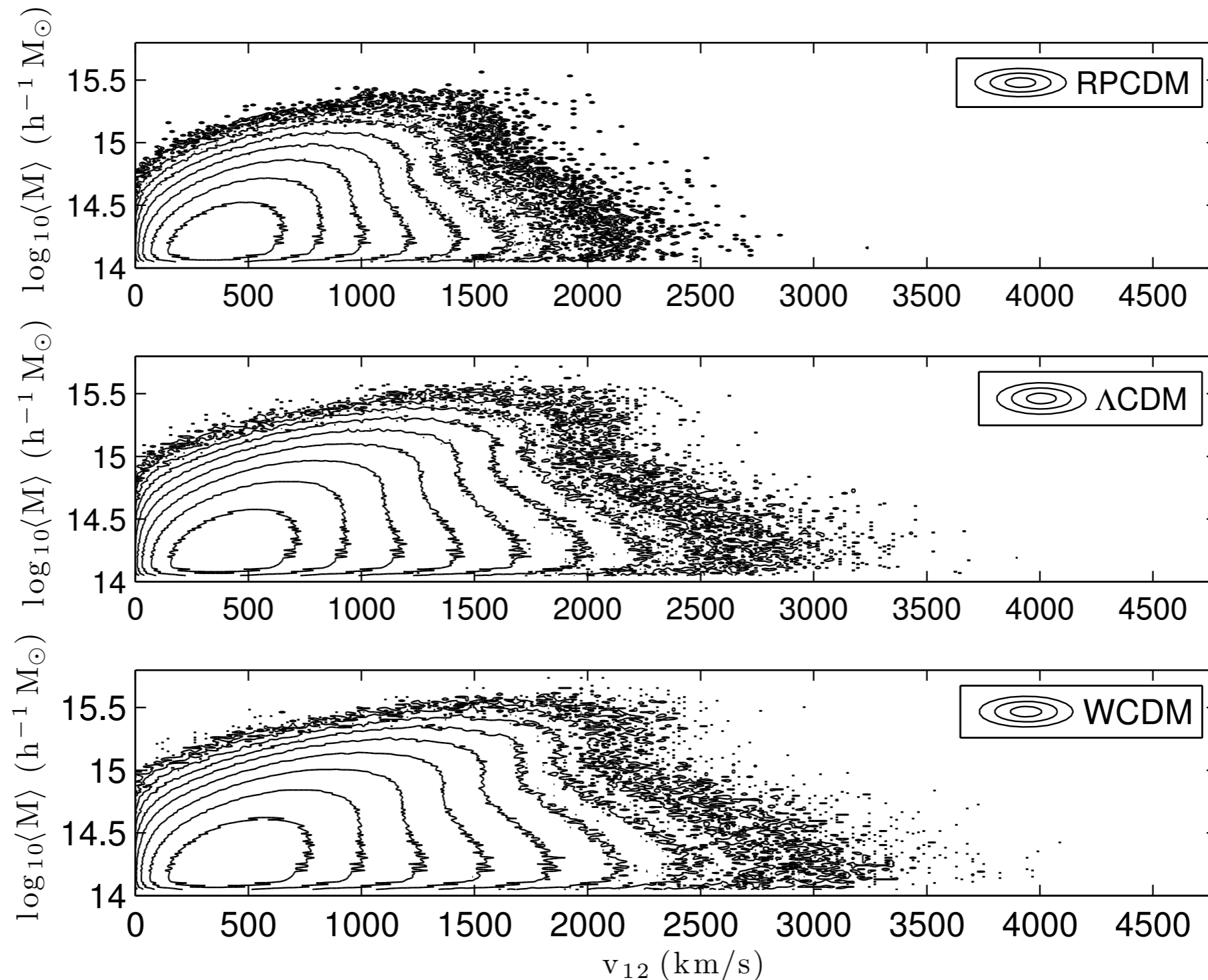
❖ Redshift dependence of (M, v_{12}) plane:

- ◆ Due to our large statistics, two regions appear in the simulations.
- ◆ In blue, standard BC: a cluster-subcluster collision.
- ◆ In red, MACS J0025.4-1222, a cluster-cluster interaction.
- ◆ Not a lot of BC candidates around blue lines...



OCCURENCE OF BULLETS

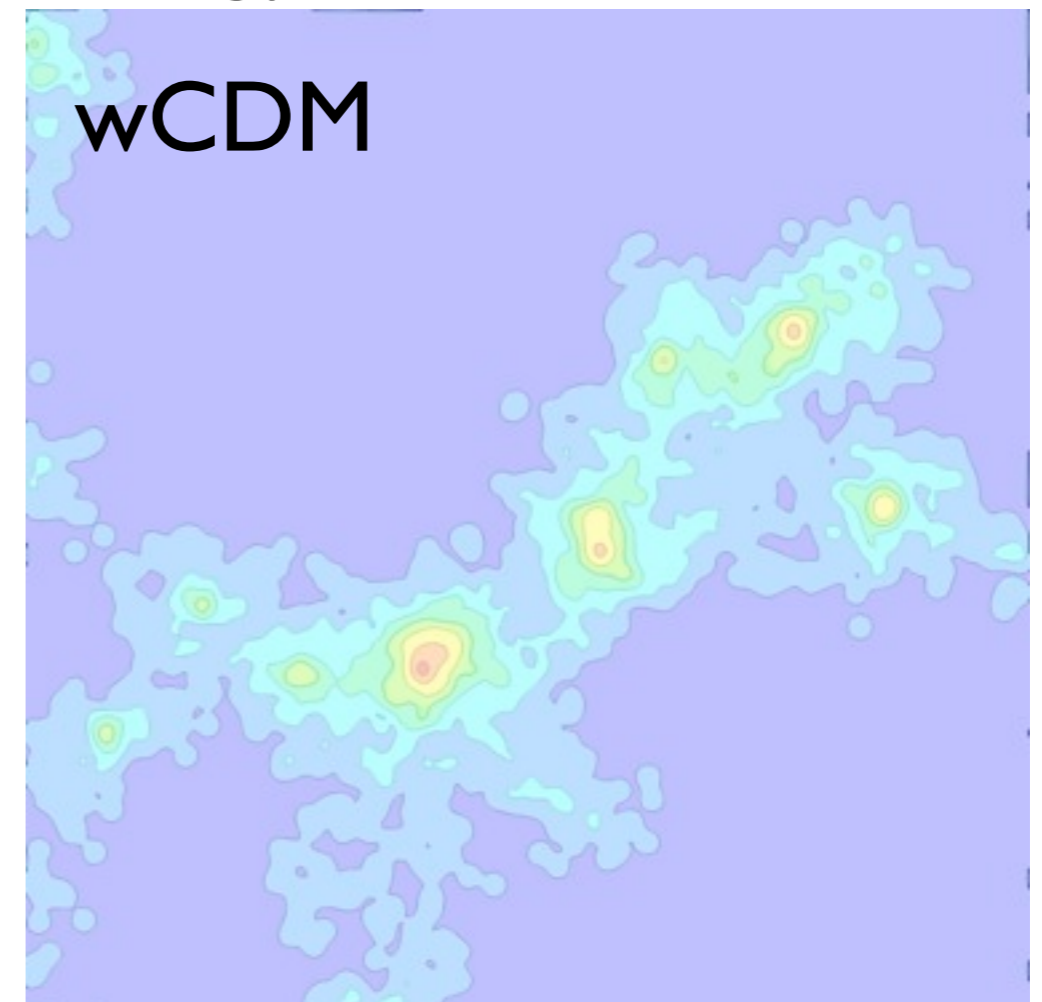
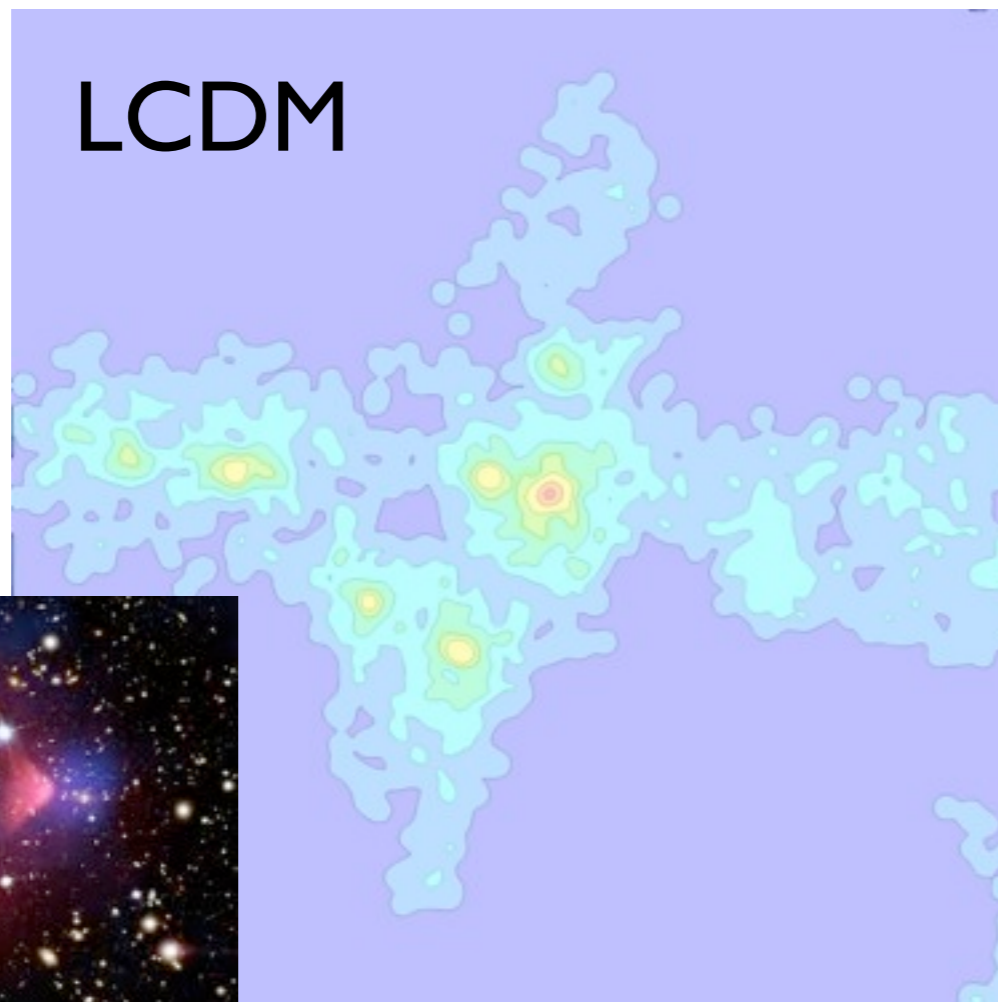
- ❖ Cosmology dependence of (M, v_{12}) plane (@ $z=0$):



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OCCURENCE OF BULLETS

- ❖ Cosmology dependence of (M, v_{12}) plane (@ $z=0$):
 - ◆ In the Ratra-Peebles model, it is NOT possible.
 - ◆ In a phantom cosmology, it is possible (many candidates).
 - ◆ The limit case is the standard cosmology (1 candidate)...





PROBABILITY OF BULLETS

- ❖ Usual approach is to model the tail of the pairwise velocity PDF as a gaussian.
- ❖ However, we already know it is not!
 - ◆ Tails of distribution have something to do with Pareto function.
 - ◆ A gaussian modeling can lead to an under-(over-)estimation of the probability of occurrence.
- ❖ Previous studies (Hayashi et al., Lee et al., Thompson et al.) use gaussians:
 - ◆ Their conclusions: the BC is impossible (10^{-9}) in LCDM model.

PROBABILITY OF BULLETS

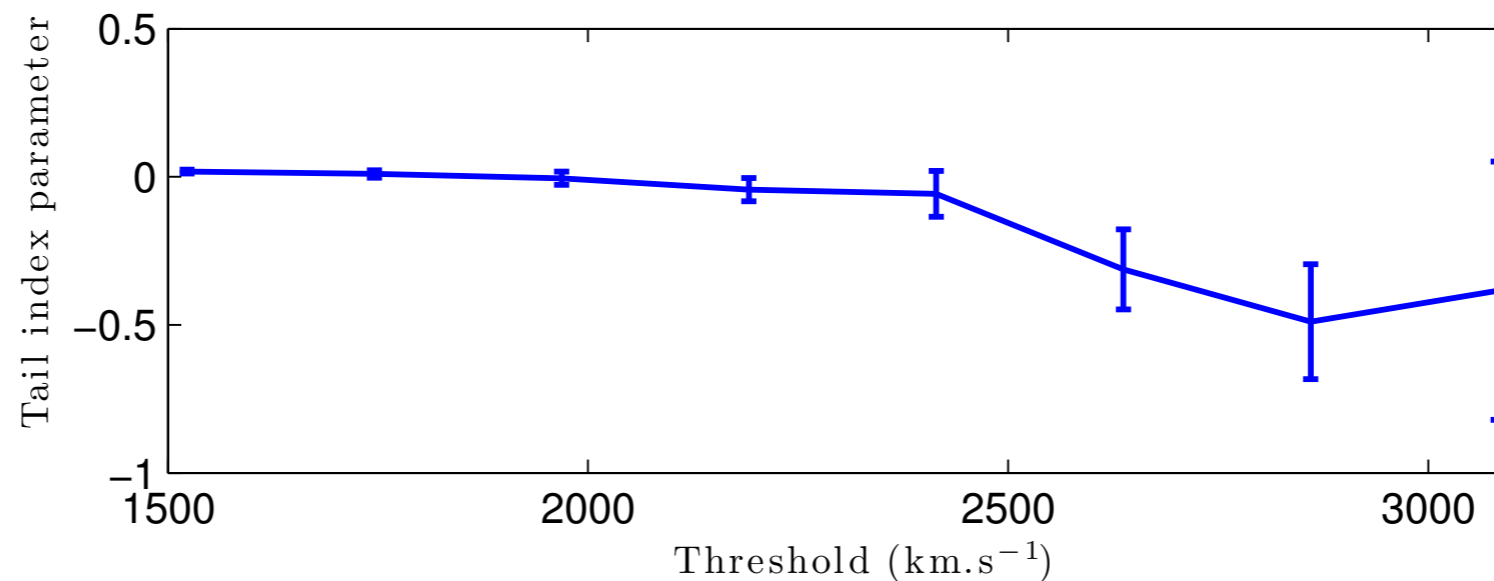
❖ Extreme value approach:

◆ Define an extremal event: choose of threshold

◆ Tail of our velocity distribution is a generalized Pareto function:

$$F_{(\xi, \mu, \sigma)}(x) = 1 - \left[1 + \xi \left(\frac{x - \mu}{\sigma} \right) \right]_{+}^{-1/\xi}$$

◆ What is the evolution of the tail index with the threshold?



PROBABILITY OF BULLETS

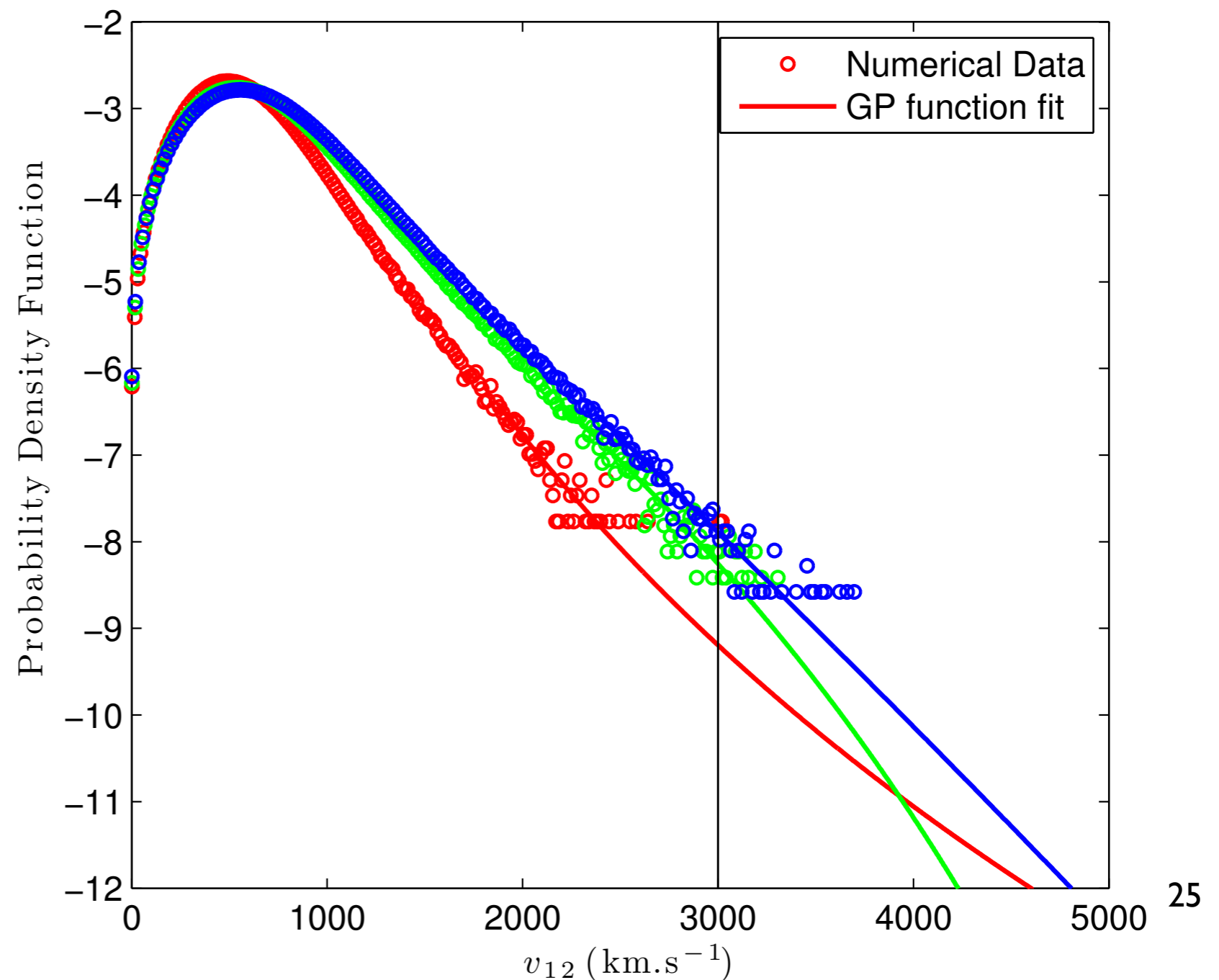
❖ The tail index is close to zero (gaussian case) but not exactly zero (10^{-2}).

❖ Higher proba of BC ($v > 3000$):

◆ RPCDM: $3 \cdot 10^{-8}$

◆ LCDM: $9 \cdot 10^{-7}$

◆ w CDM: $3 \cdot 10^{-6}$

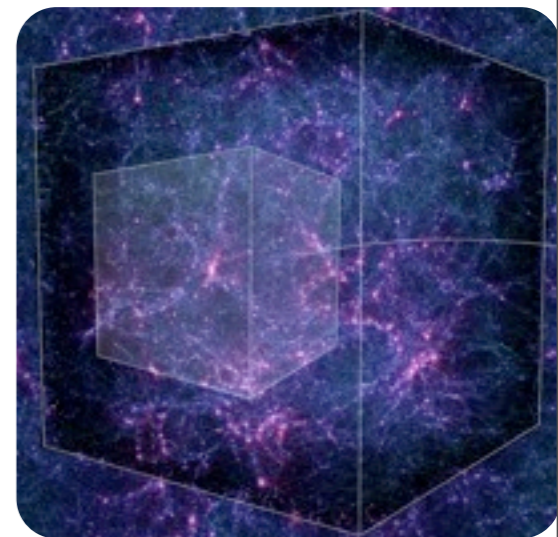


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II. LARGE SCALE COSMOLOGICAL VELOCITY FIELDS

- 1) Local Universe measurements
- 2) Numerical catalogs
- 3) Link with initial conditions



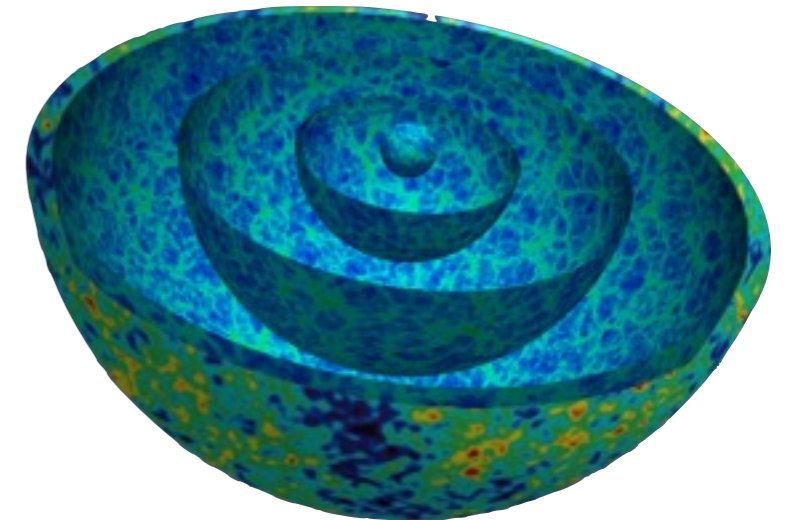
LOCAL UNIVERSE MEASUREMENTS

❖ Observational state:

- ◆ COMPOSITE (SFI++, SBF...), 2MRS, 6dF...

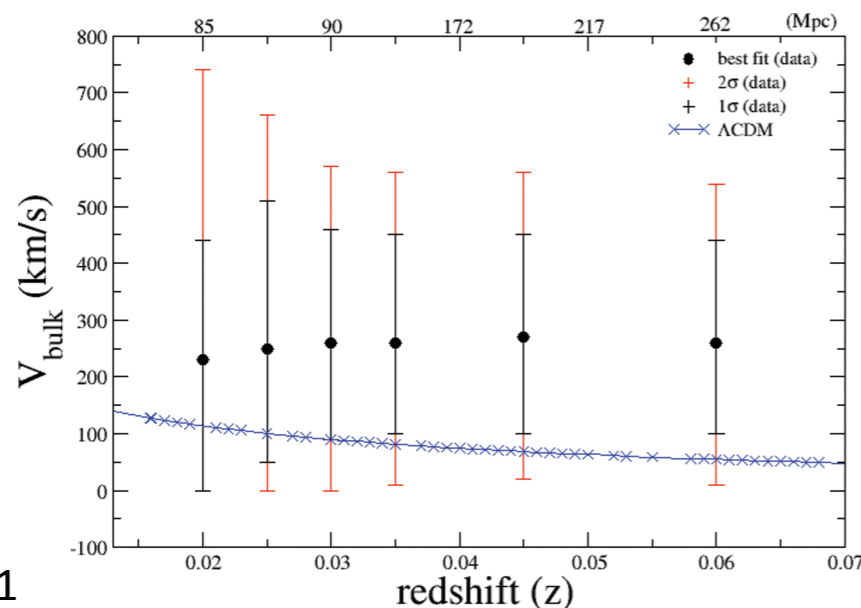
❖ Two measured facts:

- ◆ Non-reconvergence of the spherical mean of the velocity fields at large scales towards the CMB dipole.



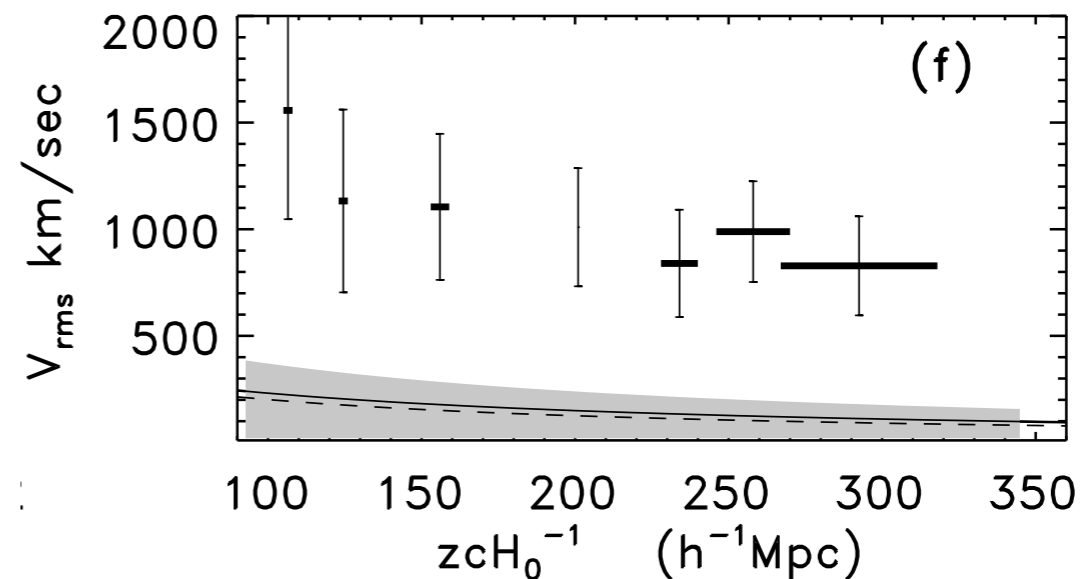
Référentiel CMB

$$\vec{v}_{CMB} = \vec{0}$$



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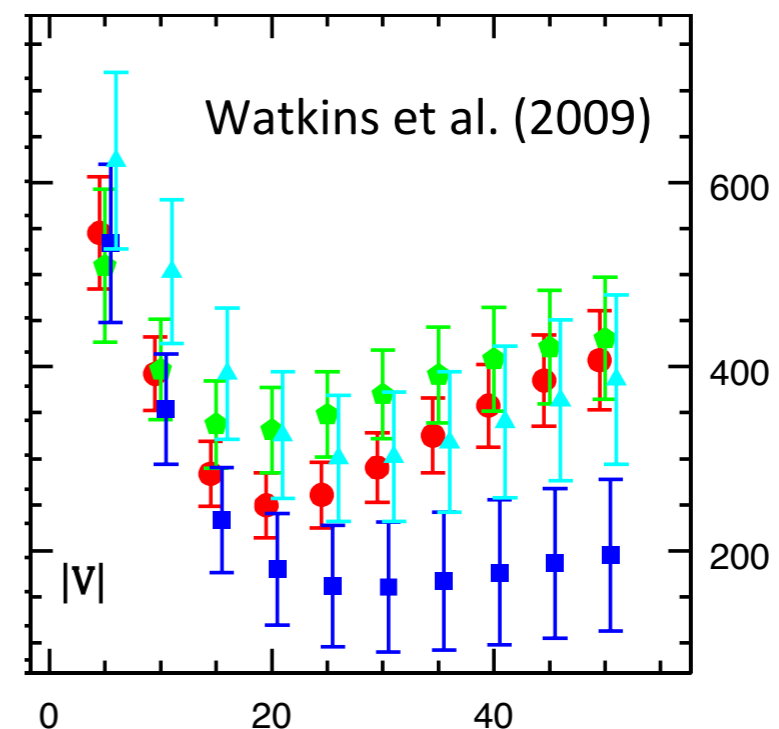
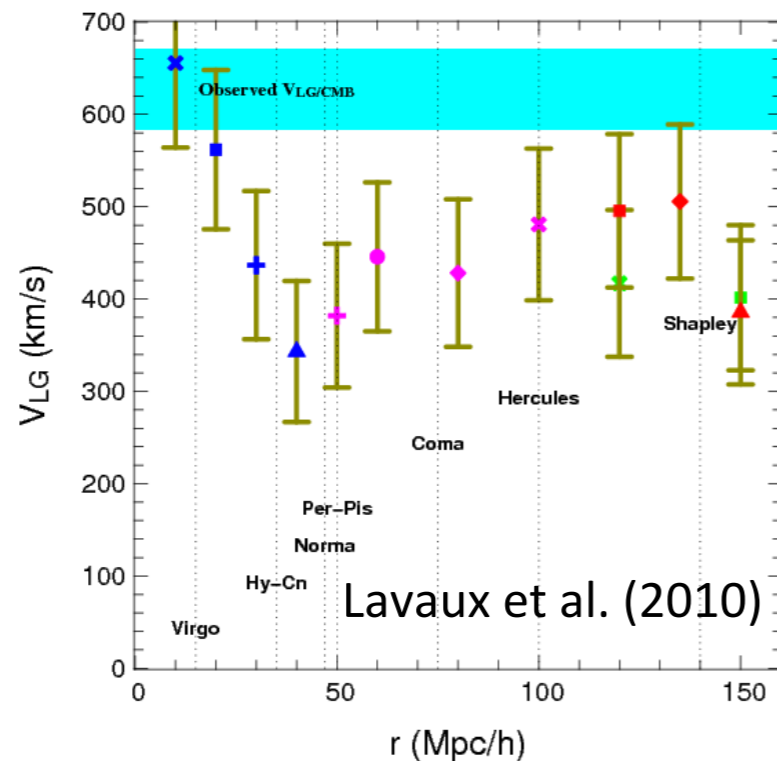
Colin et al. (2011)



Kashlinsky et al. (2008)

LOCAL UNIVERSE MEASUREMENTS

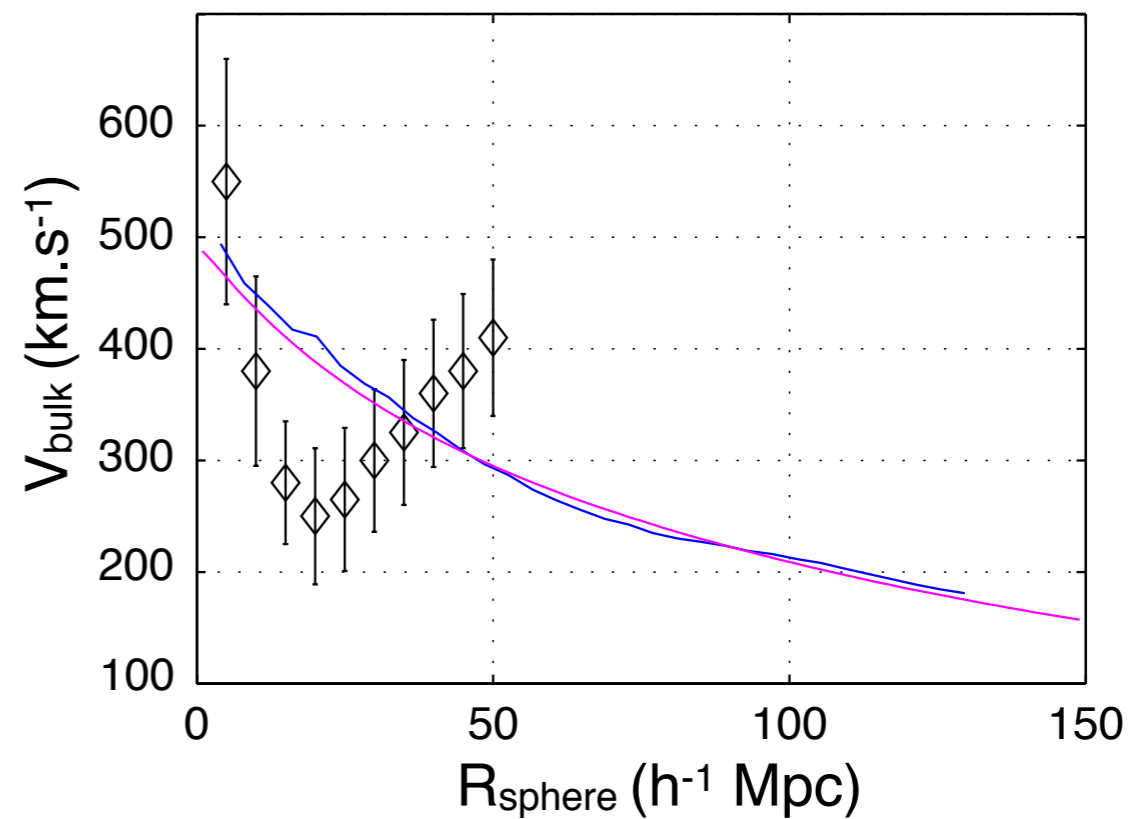
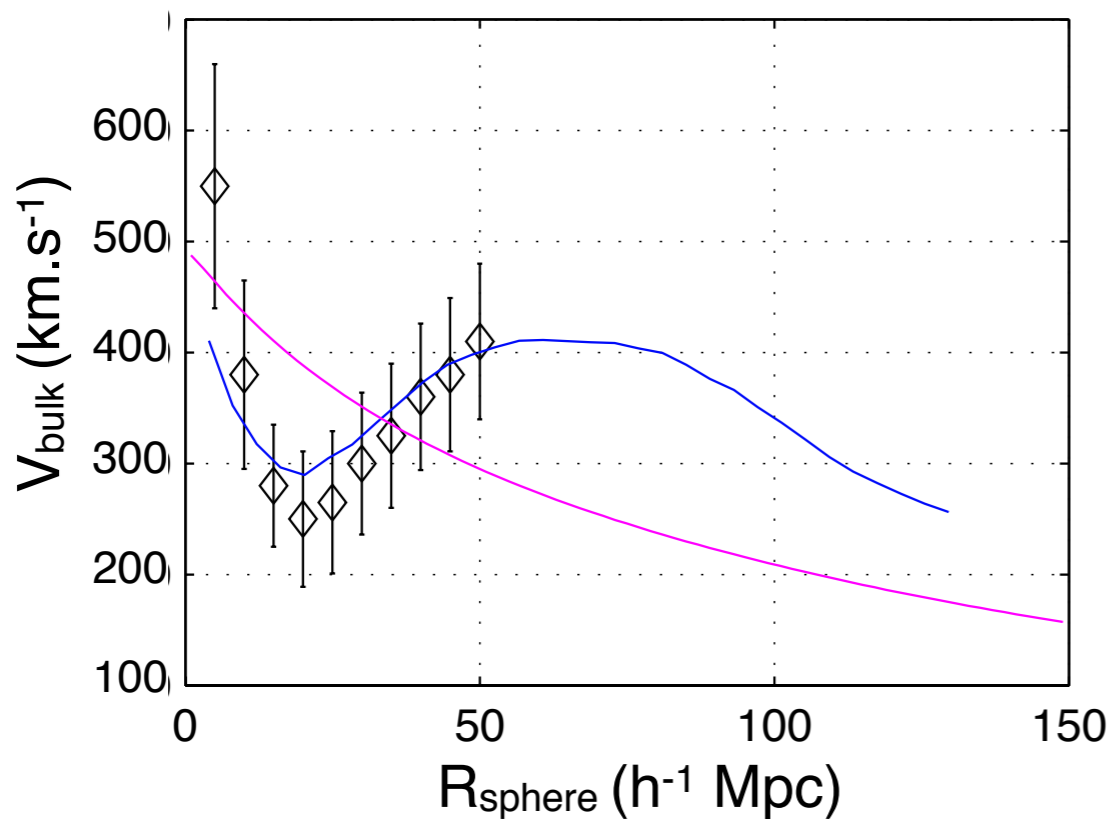
- ❖ Two measured facts:
 - ◆ Maximum of cosmic flows at intermediate scales.
- ❖ Is this an issue for Λ CDM?
 - ◆ Is there a problem with hierarchical models?
 - ◆ Explanation with dynamical or statistical arguments?



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NUMERICAL CATALOGS

- ❖ Statistical behaviour on bulk flows: build numerical catalogs in DEUSS simulations:
 - ◆ Realistic catalog: Extrema in agreement with obs.
 - ◆ Linear catalog: profile in agreement with lin. prediction.

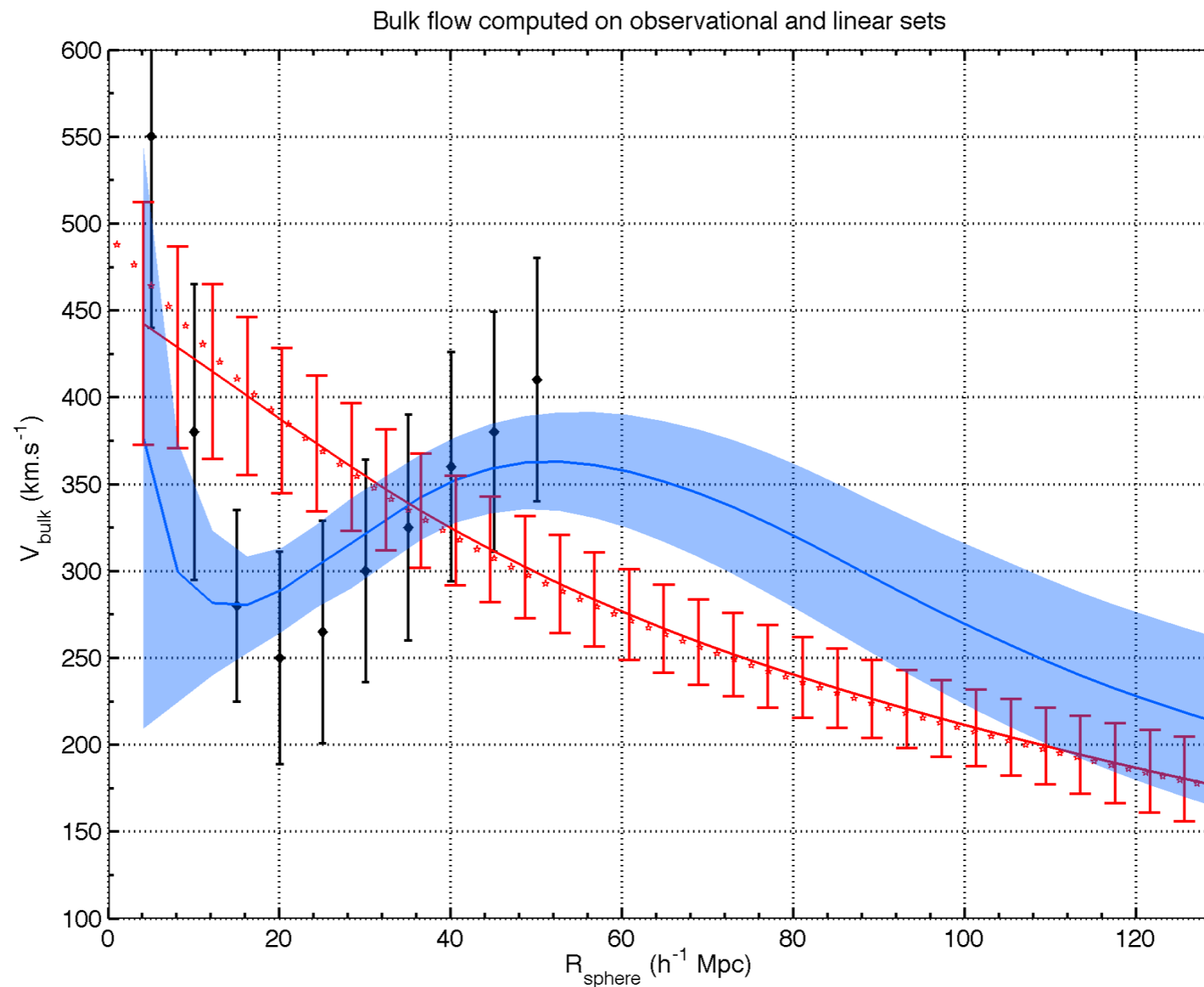


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Imprints of Dark Energy on structure formation

NUMERICAL CATALOGS

❖ Catalogs mean trend (σ_R & bulk flow):



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Imprints of Dark Energy on structure formation

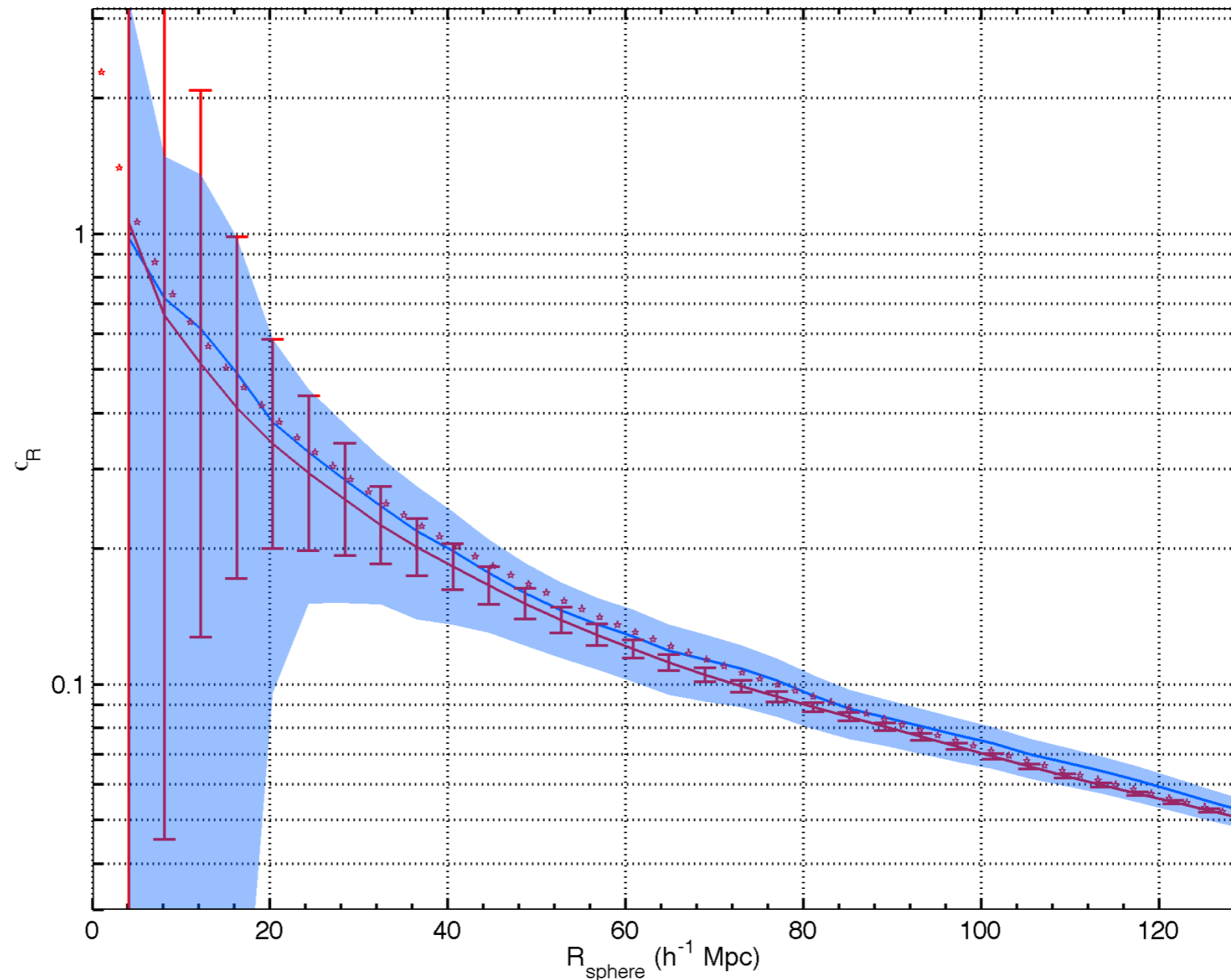
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NUMERICAL CATALOGS

❖ Catalogs mean trend (σ_R & bulk flow):

RMS mass fluctuation amplitude c_R computed on various sets



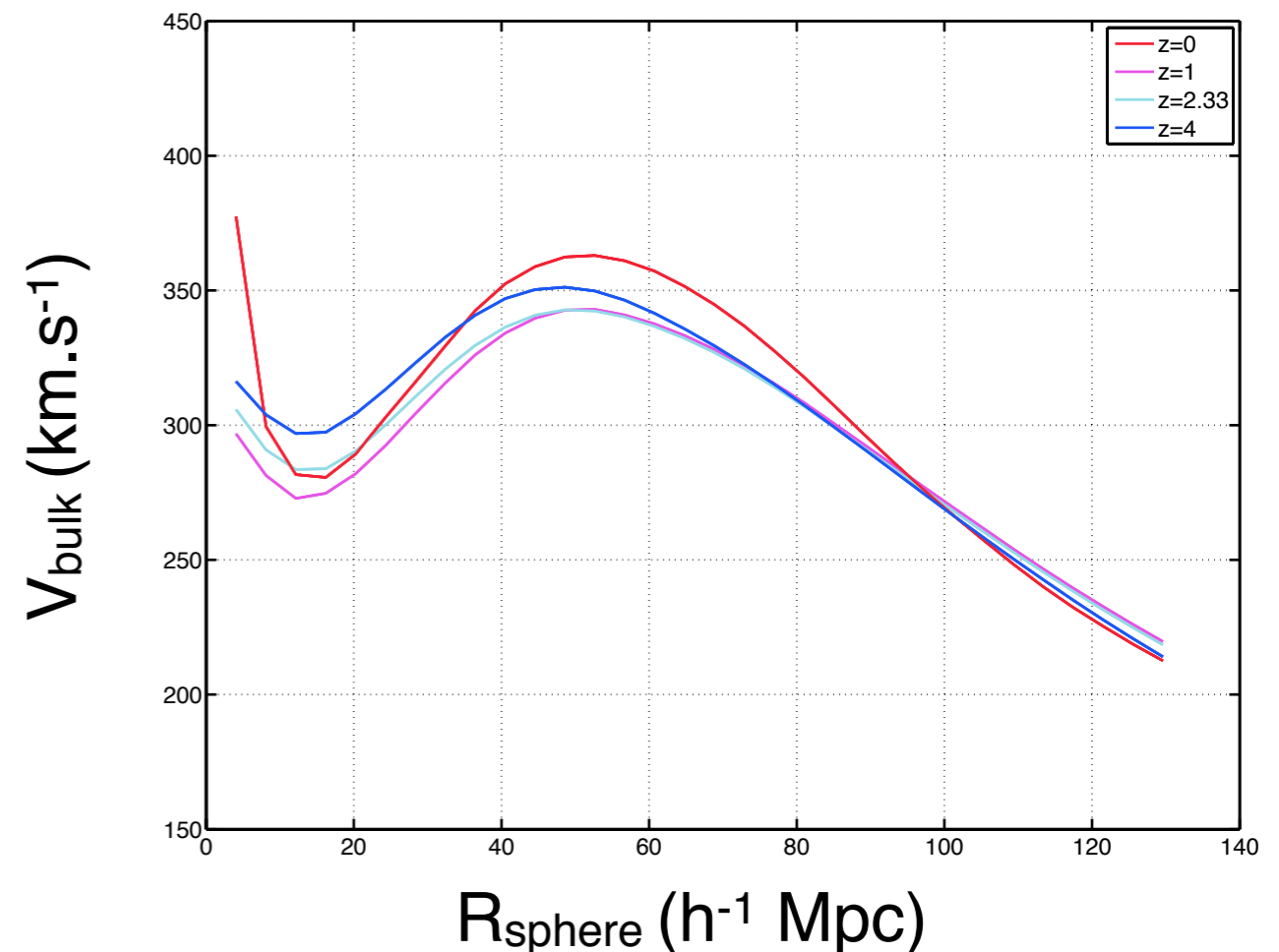
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Imprints of Dark Energy on structure formation

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LINK WITH INITIAL CONDITIONS

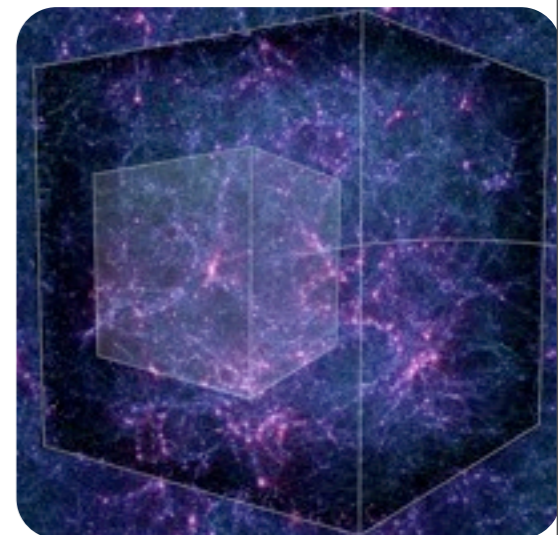
- ❖ An initial condition issue:
 - ◆ Follow the evolution backward in time of each member of catalogs.
 - ◆ Compute mean bulk flow renormalized by linear evolution factors.
 - ◆ The bulk flow stays the same through time: it results from a linear evolution.





III. STATISTICAL INTERPRETATION OF A HIGH VELOCITY COSMIC FLOWS

- 1) Bulk flow prediction: 1-point pdf
- 2) Bulk flow: N-point pdf
- 3) Bulk flow linear deviation: 2-point pdf
- 4) Retrieving cosmology: 3-point pdf



BULK FLOW: 1-POINT PDF

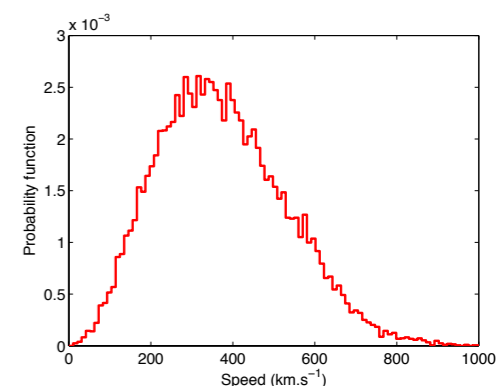
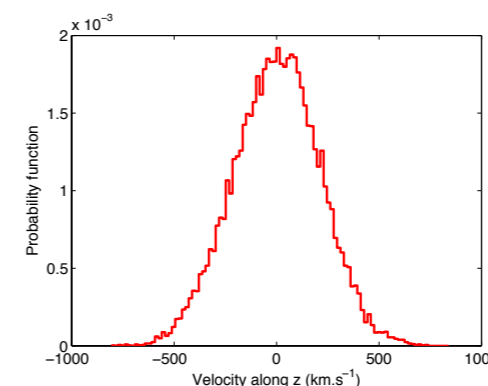
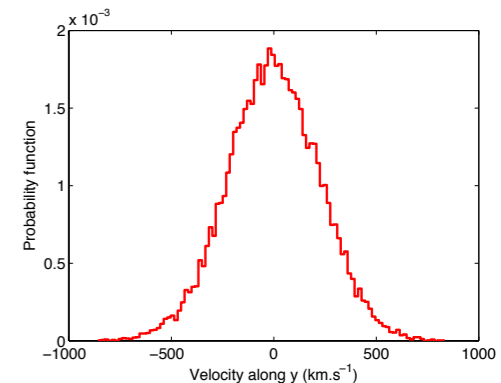
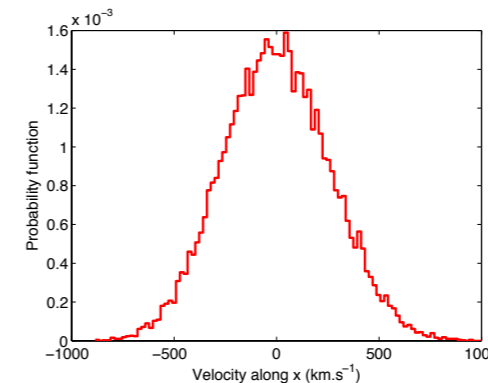
- ❖ Gaussian initial conditions in a given model: what is the probability to have a bulk flow \vec{v}_1 in a sphere of radius R_1 ?
- ❖ Standard issue in the kinetic theory of gases:

$$\begin{aligned} P(\vec{v}_1) d^3 \vec{v}_1 &= P(v_{1,x}, v_{1,y}, v_{1,z}) dv_{1,x} dv_{1,y} dv_{1,z} \\ &= P(v_{1,x}) dv_{1,x} P(v_{1,y}) dv_{1,y} P(v_{1,z}) dv_{1,z} \end{aligned}$$

- ◆ $v_{1,j}$ is gaussian: its norm is a Maxwell-Boltzmann distribution:

$$P(v_1) = 4\pi \left(\frac{1}{\sigma_R \sqrt{2\pi}} \right)^3 v_1^2 \exp \left(-\frac{1}{2} \frac{v_1^2}{\sigma_R^2} \right)$$

$$\sigma_R^2 = \frac{1}{6\pi^2} \int_0^\infty k^3 P_v(k) \hat{W}(kR_1)^2 \frac{dk}{k}$$



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BULK FLOW: N-POINT PDF

- ❖ Let $\vec{V} = (\vec{v}_1, \vec{v}_2, \dots, \vec{v}_N)$ a set of bulk flows at N radii.
 - ◆ What is the probability to get a particular set of bulk flows in a given cosmology \mathcal{C} ?

- ❖ Quantification of correlations between scales:

$$\langle \vec{v}_{k,i} \cdot \vec{v}_{k',i} \rangle = \delta^{k,k'} \sigma_i^2$$
$$\langle \vec{v}_{k,i} \cdot \vec{v}_{k',j} \rangle = \delta^{k,k'} \gamma_{i,j} \sigma_i \sigma_j$$

- ❖ Gaussian initial conditions:

$$\sigma_i^2 = \frac{1}{6\pi^2} \int_0^\infty k^3 P_v(k) \hat{W}(kR_i)^2 \frac{dk}{k}$$
$$\gamma_{i,j} = \frac{1}{6\pi^2 \sigma_i \sigma_j} \int_0^\infty k^3 P_v(k) \hat{W}(kR_i) \hat{W}(kR_j) \frac{dk}{k}$$

BULK FLOW: N-POINT PDF

❖ Simplification: reduced variables $\vec{U}_i = \vec{V}_i / \sigma_i$.

◆ For the k-th component of the bulk flow vector:

$$P(V_k | \mathcal{C}) = \frac{1}{(2\pi)^{N/2} \sqrt{|\mathcal{C}|}} \prod_i \left(\frac{1}{\sigma_i} \right) \exp \left(-\frac{1}{2} U_k^\dagger \mathcal{C}^{-1} U_k \right)$$

with \mathcal{C} the covariance matrix linking scales:

$$\mathcal{C} = \begin{pmatrix} 1 & & \gamma_{j,i} \\ & \ddots & \\ \gamma_{i,j} & & 1 \end{pmatrix}$$

◆ Independence of the x, y, z components:

$$P(\vec{V} | \mathcal{C}) = \frac{|\mathcal{C}^{-1}|^{3/2}}{(2\pi)^{3N/2}} \prod_i \left(\frac{1}{\sigma_i} \right)^3 \exp \left(-\frac{1}{2} \sum_{k=1}^3 U_k^\dagger \mathcal{C}^{-1} U_k \right)$$

BULK FLOW: N-POINT PDF

- ❖ Quantify the norm of the bulk flow:
 - ◆ Introduce the relative angle α_{ij} between directions i and j of the bulk flow in spherical coordinates ($M=C^{-1}$):

$$dP(v_1, \dots, v_i, \dots, v_N | \mathcal{C}) = \frac{|C^{-1}|^{3/2}}{(2\pi)^{3N/2}} \prod_i \left(\frac{1}{\sigma_i} \right)^3 \exp \left(-\frac{1}{2} \sum_i m_{i,i} U_i^2 \right) \\ \times \exp \left(-\frac{1}{2} \sum_{\substack{i,j \\ i \neq j}} m_{i,j} U_i U_j \cos(\alpha_{ij}) \right) \times \prod_i \sigma_i^3 \sin(\theta_i) U_i^2 dU_i d\theta_i d\phi_i$$

BULK FLOW: N-POINT PDF

❖ What is the probability to get a given cosmic flows profile?

◆ To marginalize on the angles, we need to know the link between spherical coordinates of v_i and α_{ij} :

$$\cos \alpha_{ij} = \sin \theta_i \sin \theta_j (\cos \phi_i \cos \phi_j + \sin \phi_i \sin \phi_j) + \cos \theta_i \cos \theta_j$$

◆ A simplification is possible under axes rotation in some cases:

▶ 2-point pdf:

$$\theta_1 = 0$$

any ϕ_1

$$\theta_2 = \alpha_{12}$$

any ϕ_2

▶ 3-point pdf:

$$\theta_1 = \phi_3 = 0$$

any ϕ_1

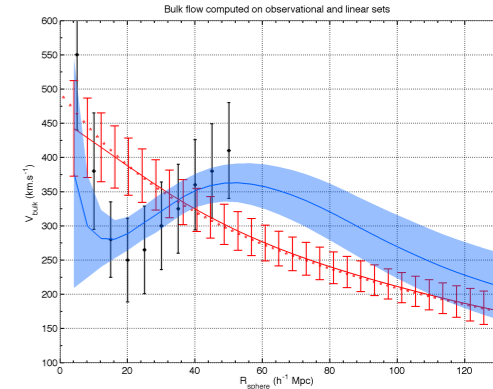
$$\cos \alpha_{12} = \cos \theta_2$$

$$\cos \alpha_{13} = \cos \theta_3$$

$$\cos \alpha_{23} = \sin \theta_2 \sin \theta_3 \cos \phi_2 + \cos \theta_2 \cos \theta_3$$

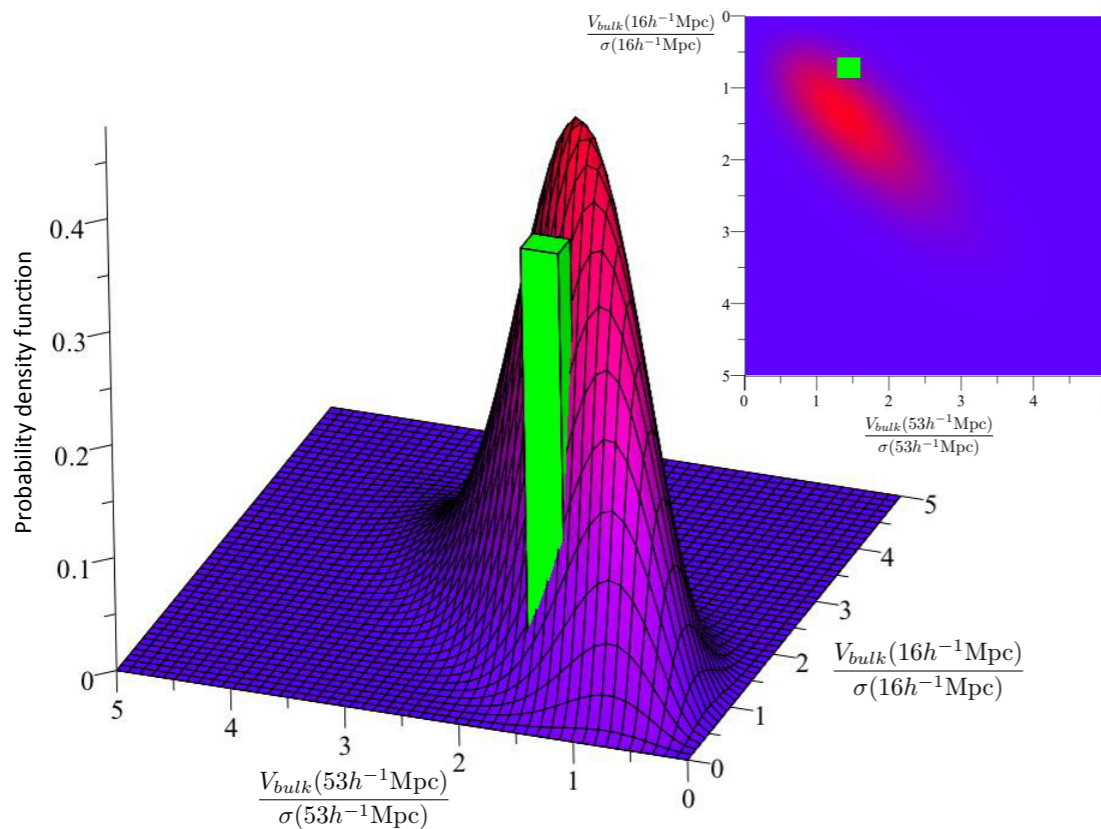
(+circ. perm)

BULK FLOW: 2-POINT PDF



- ❖ What is the probability to observe a given bulk flow profile as Watkins et al.?

$$P(v_1, v_2 | \mathcal{C}) = \frac{2}{\pi} \frac{1}{\gamma_{1,2}} \frac{1}{\sqrt{1 - \gamma_{1,2}^2}} U_1 U_2 \exp\left(-\frac{U_1^2 + U_2^2}{2(1 - \gamma_{1,2}^2)}\right) \sinh\left(\frac{\gamma_{1,2} U_1 U_2}{1 - \gamma_{1,2}^2}\right)$$



	Proba th.	Proba num.
Λ CDM	1.58%	1.56%
SUCDM	1.27%	1.17%
RPCDM	0.95%	0.82%



BULK FLOW: 2-POINT PDF

- ❖ The probability to observe such a bulk flow is low:
 - ◆ This is a rare event in a given cosmology.
 - ◆ Coherent picture between numerical and statistical points of view.
- ❖ In all cosmological models, such observations are predicted by linear theory but are proved to be rare.
- ❖ How can we retrieve the cosmological information?



BULK FLOW: 3-POINT PDF

- ❖ Have to do deeper survey until a scale R_3 : the scale of reconvergence to the linear prediction is a cosmological probe.
- ❖ Method: this hypothetical scale of reconvergence is varying.
- ❖ Probability of 3 bulk flows at 3 scales: 3-point pdf.
 - ◆ Strong correlation between 3 bulk flow vectors.
 - ◆ 3 relative angles: non-separable integration.
- ❖ Hypothesis: two relative angles are small.

BULK FLOW: 3-POINT PDF

❖ 3-point PDF:

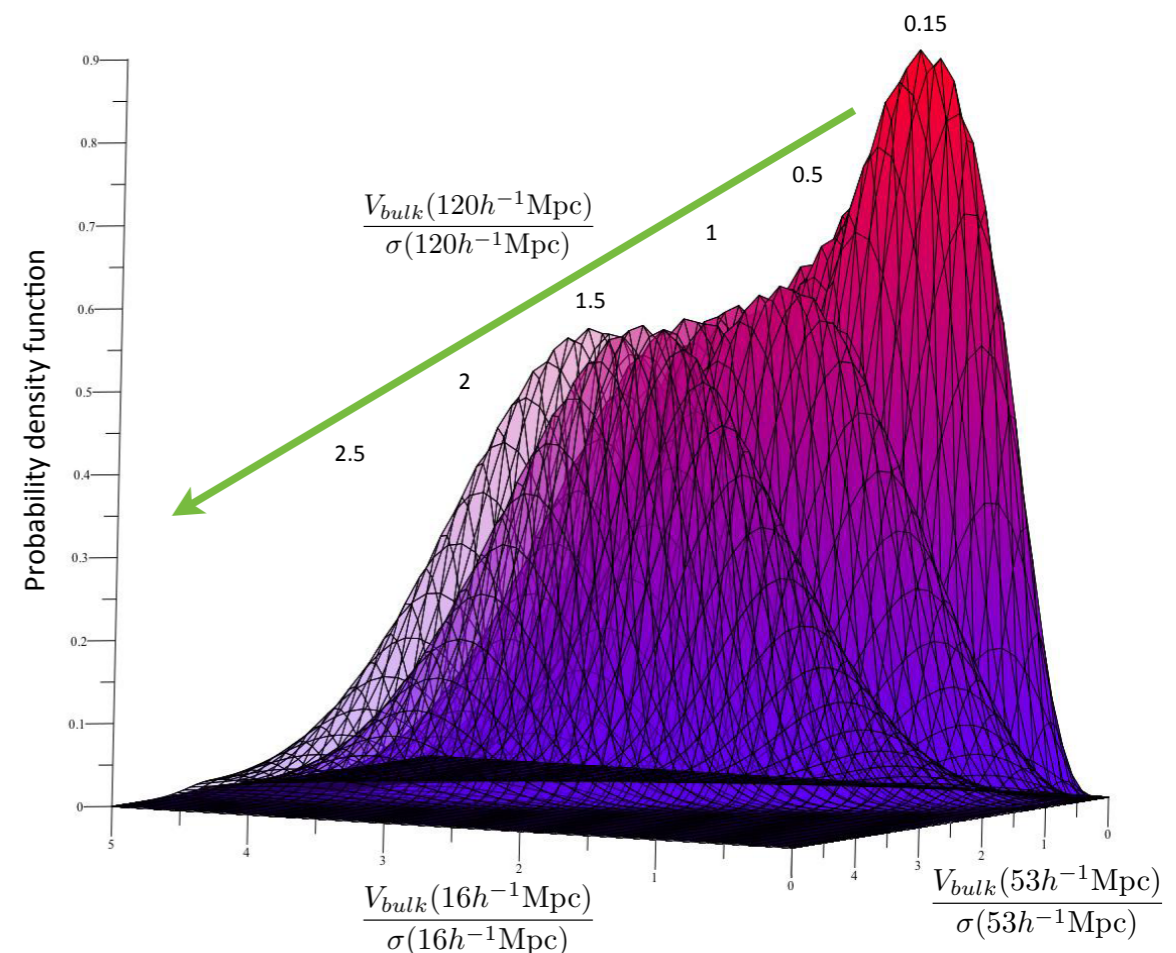
$$P(v_1, v_2, v_3 | \mathcal{C}) = \frac{2\sqrt{2}}{\pi^{3/2} m_{1,2} m_{1,3}} U_2 U_3 |C^{-1}|^{3/2} \exp\left(-\frac{1}{2} (m_{1,1} U_1^2 + m_{2,2} U_2^2 + m_{3,3} U_3^2)\right) \\ \times \sinh(U_1 U_2 m_{1,2}) \sinh(U_1 U_3 m_{1,3}) \times \mathcal{I}_0(U_2 U_3 m_{2,3}) + \text{perm. circ.}$$

❖ The differential probability of reconvergence is given by:

$$P(v_3 | v_1, v_2) = \frac{P(v_1, v_2, v_3)}{P(v_1, v_2)}$$

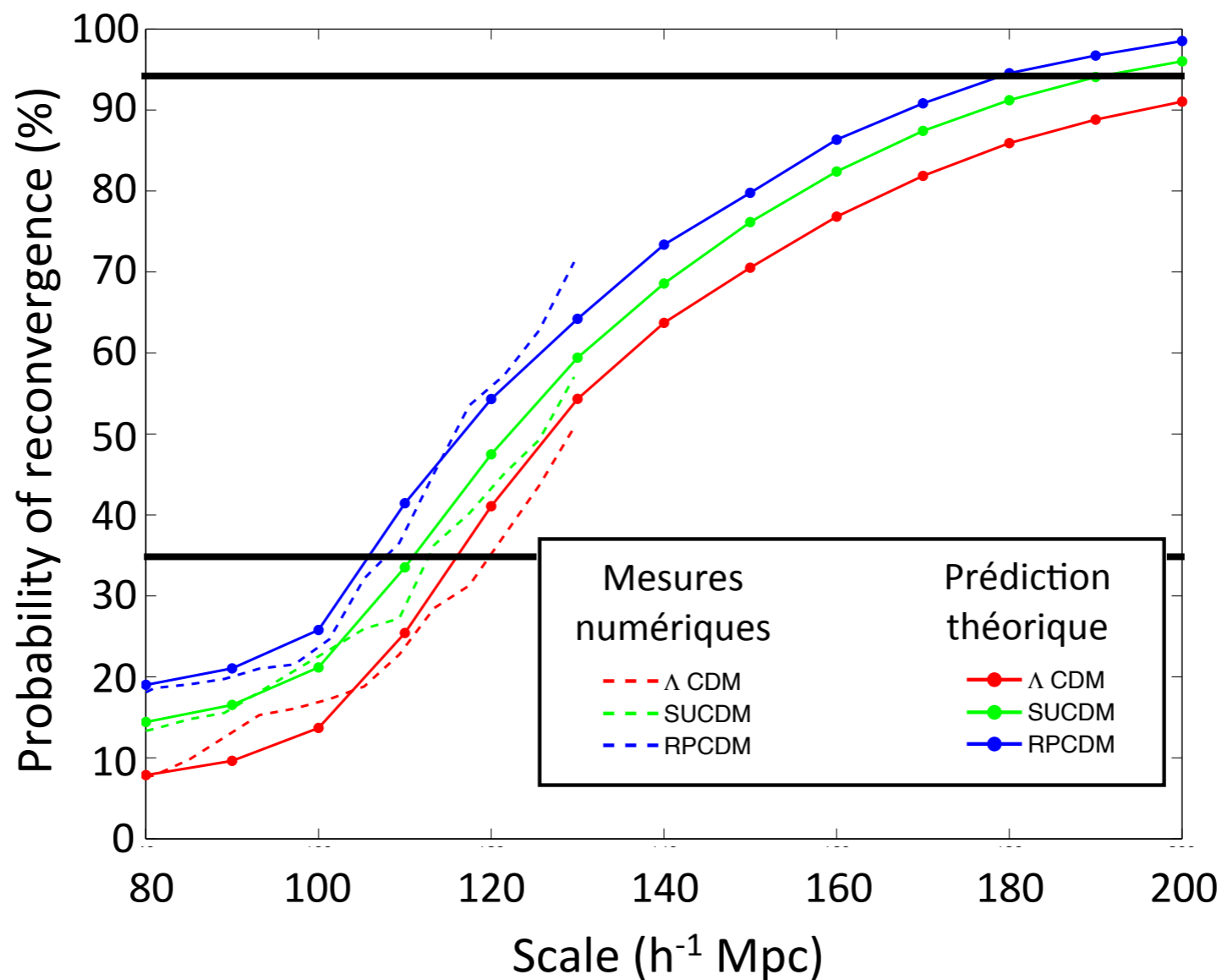
❖ The probability of reconvergence is given by:

$$Q(v_3 | v_1, v_2) = \int_0^{v_3} \frac{P(v_1, v_2, u)}{P(v_1, v_2)} du$$



BULK FLOW: 3-POINT PDF

- ❖ An original cosmological probe:
 - ◆ The scale of reconvergence to linear theory @ 95%.



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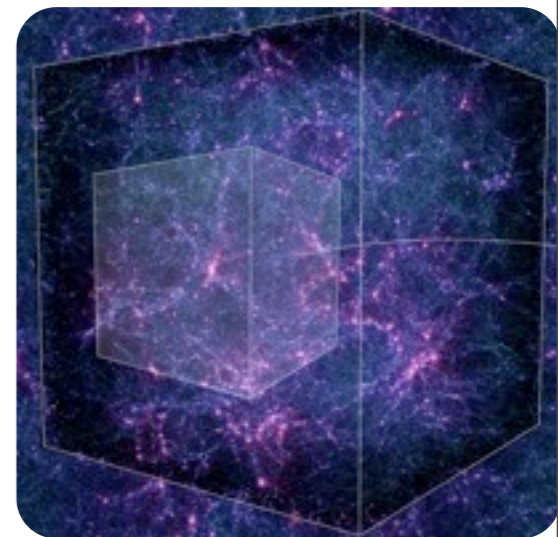
CONCLUSIONS (SO FAR)

- ❖ Large bulk flows in apparent disagreement with linear theory at large scales: a problem for hierarchical CDM models?
- ❖ High cosmic flows come from a statistically rare event ($\sim 1\%$) in agreement with the linear theory and consistent with numerical simulations.
- ❖ This rare feature gives birth to an original cosmological probe.



IV. LARGE-SCALE ASYMMETRY: ORIGIN OF HIGH VELOCITY COSMIC FLOWS

- 1) Qualitative approach of density field
- 2) Quantitative approach: asymmetry index
- 3) A characteristic scale



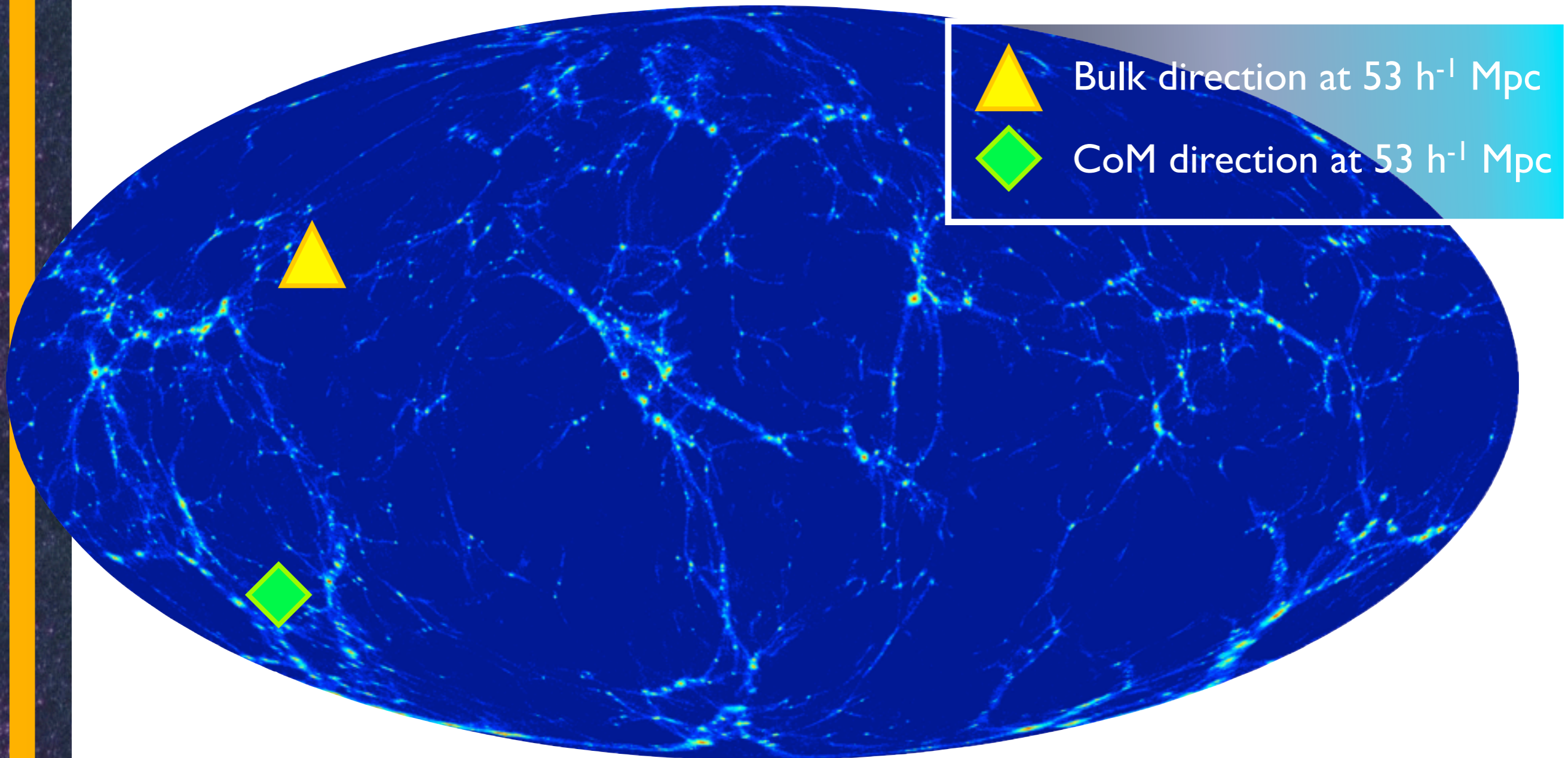


QUALITATIVE APPROACH

- ❖ Reconvergence of the bulk flow intuitively linked with an homogenization of the density field at higher scales:
 - ◆ What is the dynamical origin of the high velocity bulk flow at intermediate scales in a rare environment?
 - ◆ How to characterize the density field to find this origin?
- ❖ Bulk flow is a vector (i.e. a directional quantity):
 - ◆ For the density field, a direction can be introduced: the center of mass of a sphere.

QUALITATIVE APPROACH

- ❖ Example: Mollweide projection ($53 h^{-1} \text{ Mpc}$)



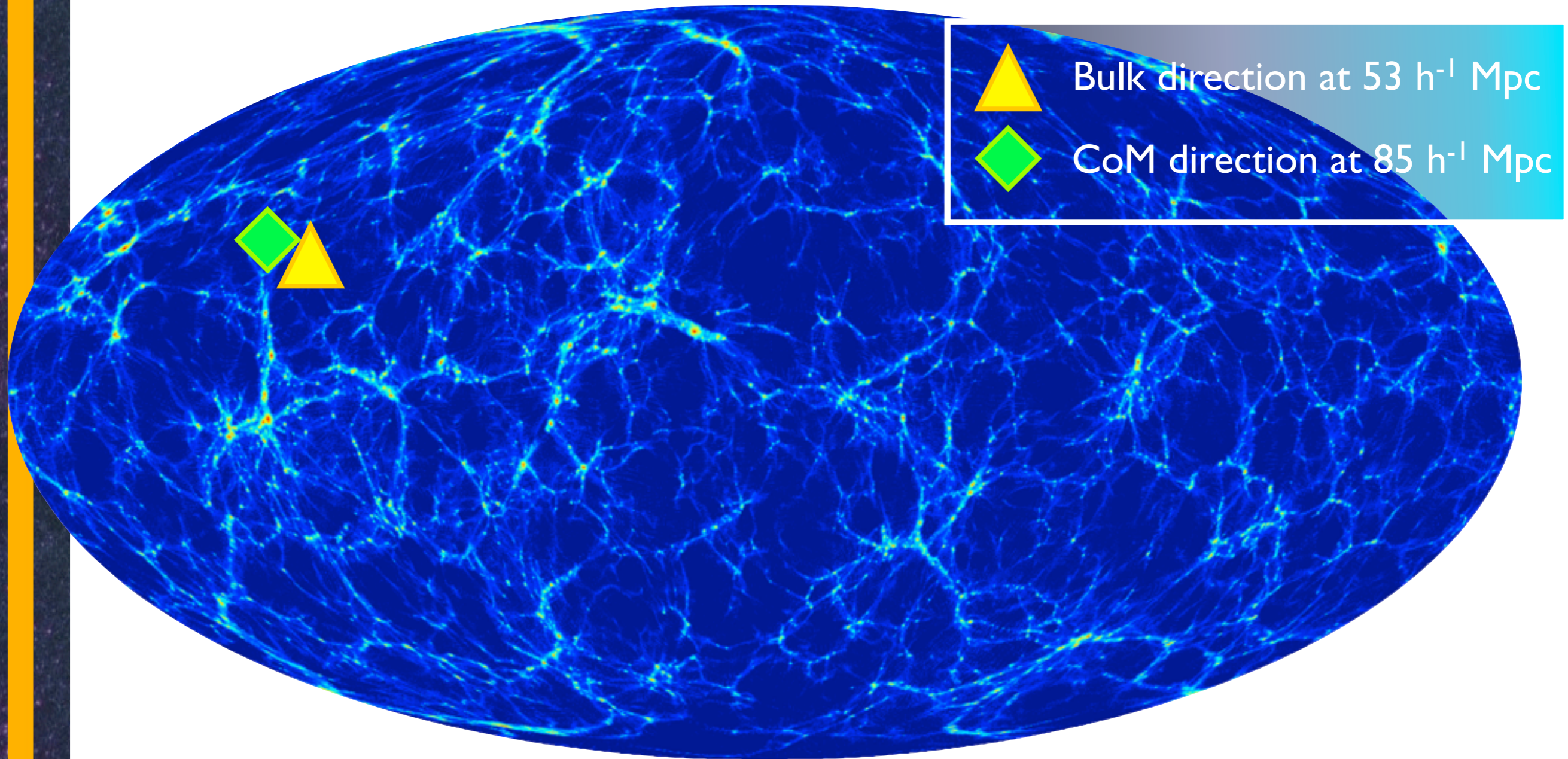
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Imprints of Dark Energy on structure formation

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QUALITATIVE APPROACH

- ❖ Example: Mollweide projection ($85 h^{-1} \text{ Mpc}$)



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Imprints of Dark Energy on structure formation

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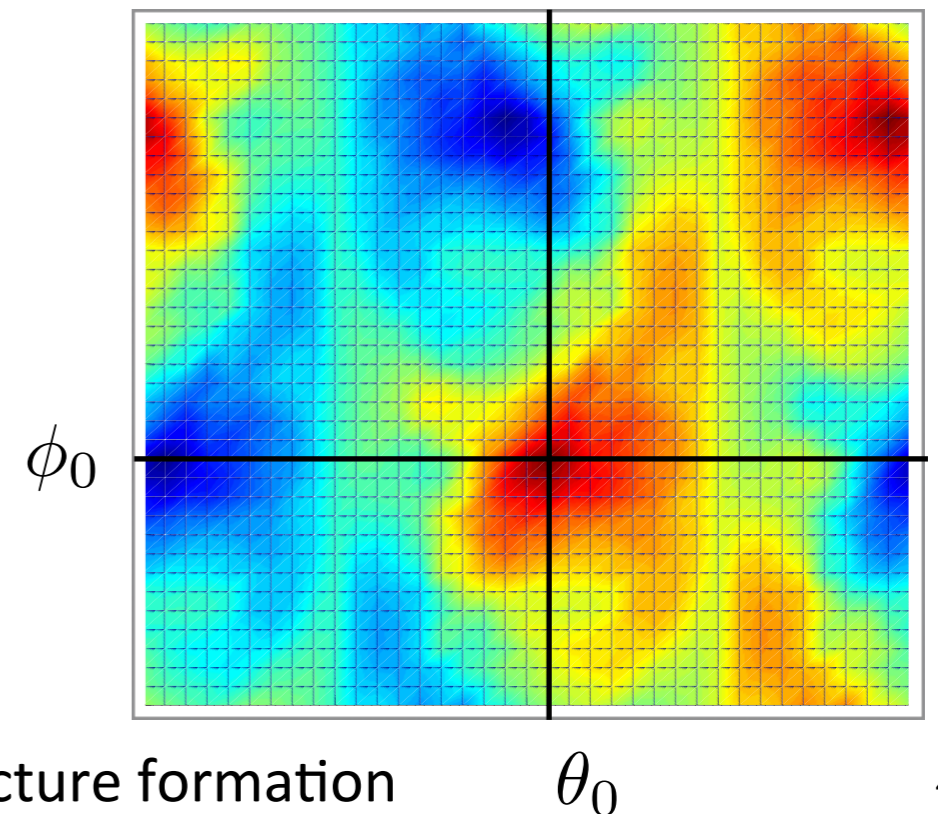
QUANTITATIVE APPROACH

- ❖ The center of mass approach suffers from many issues (e.g. normalisation problem).
- ❖ More accurate and efficient tool: an estimator of asymmetry of spheres (or shells).

$$F_R(\theta_0, \phi_0) = \frac{1}{\rho_{tot}} \iint_{\mathbb{S}^2/2} \rho_R(\theta + \theta_0, \phi + \phi_0) - \rho_R(\pi - (\theta + \theta_0), \pi + (\phi + \phi_0)) d\Omega$$

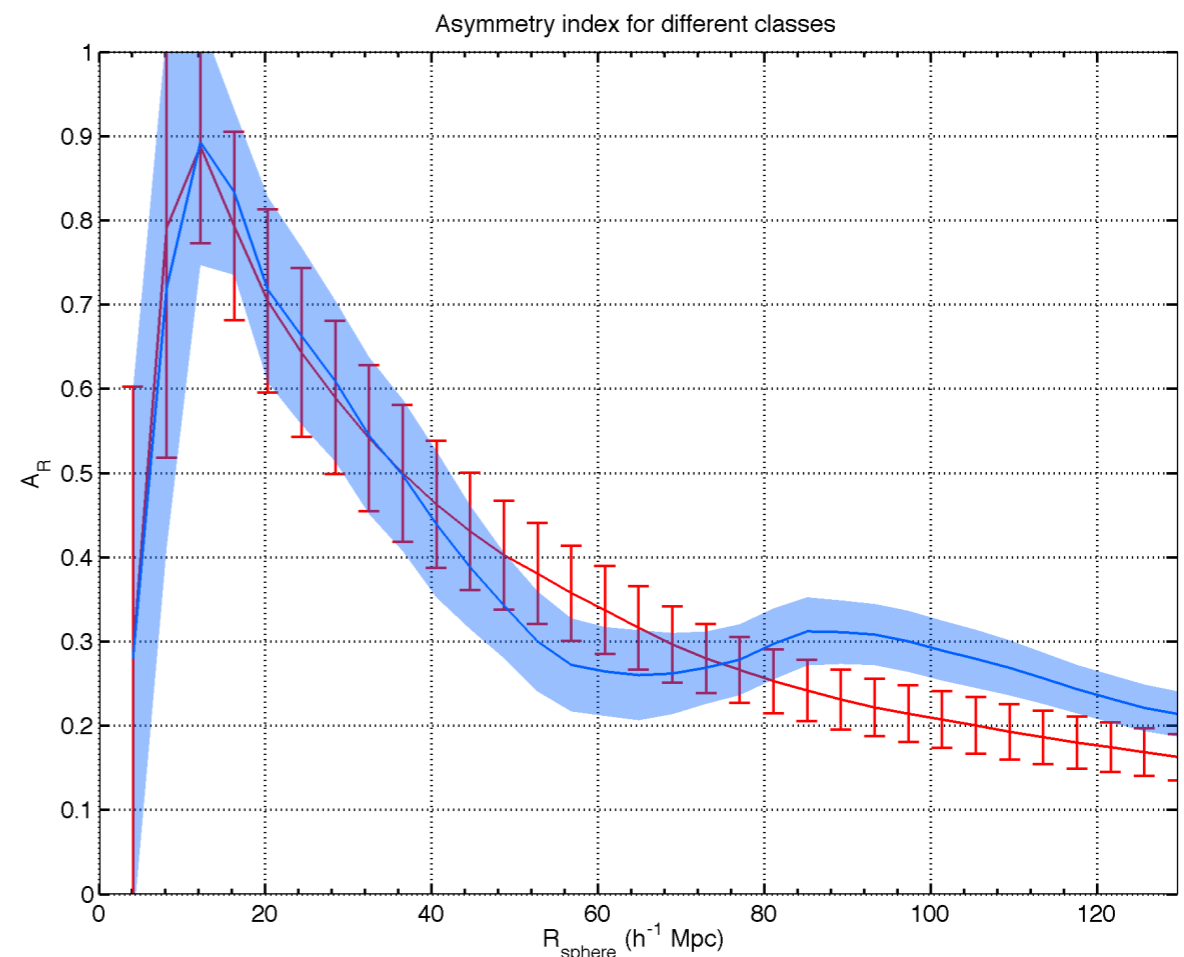
$$A_R = \max_{\phi_0 \in [0, 2\pi], \theta_0 \in [0, 2\pi]} F_R(\theta_0, \phi_0)$$

- ❖ Direction of the asymmetry A_R given by (ϕ_0, θ_0) .



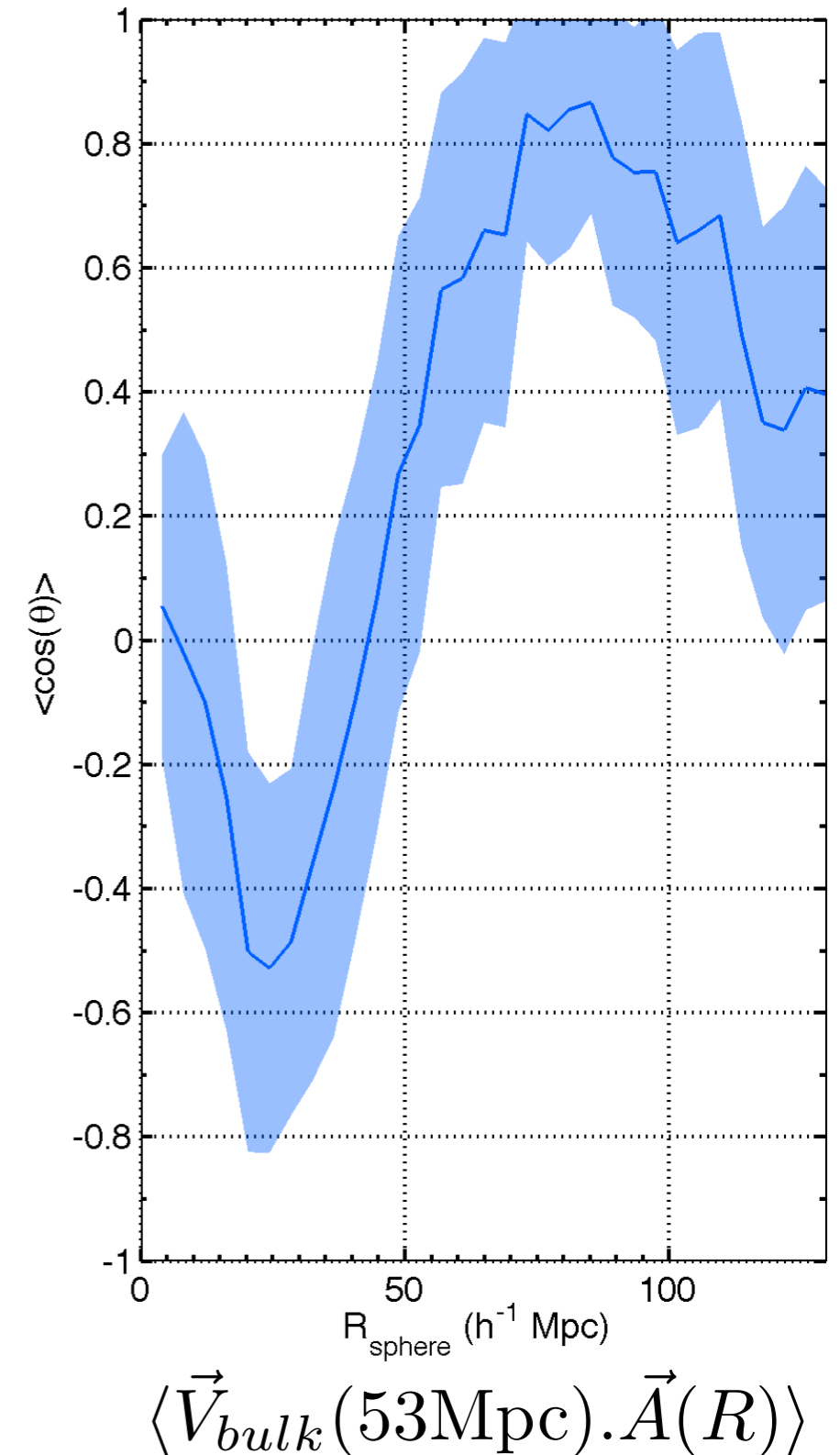
QUANTITATIVE APPROACH

- ❖ Mean of asymmetry indexes on linear (red) and realistic (blue) numerical catalogs in spheres.
- ❖ Two particular scales for the realistic catalog:
 - ◆ Depletion @ $60 h^{-1}$ Mpc.
 - ◆ Bump @ $85 h^{-1}$ Mpc.
- ❖ Link between this bump of asymmetry and the bump of bulk flow?



A CHARACTERISTIC SCALE

- ❖ Alignment between the bulk flow at $53 h^{-1} \text{ Mpc}$ and the asymmetry vector in shells at radius R ?
- ◆ Realistic catalog: scales between 60 and $100 h^{-1} \text{ Mpc}$, peaking at $85 h^{-1} \text{ Mpc}$.
- ◆ Linear catalog: no particular scales.
- ❖ Perfect alignment of the bulk flow at $53 h^{-1} \text{ Mpc}$ and the asymmetry in shells at radius $85 h^{-1} \text{ Mpc}$.



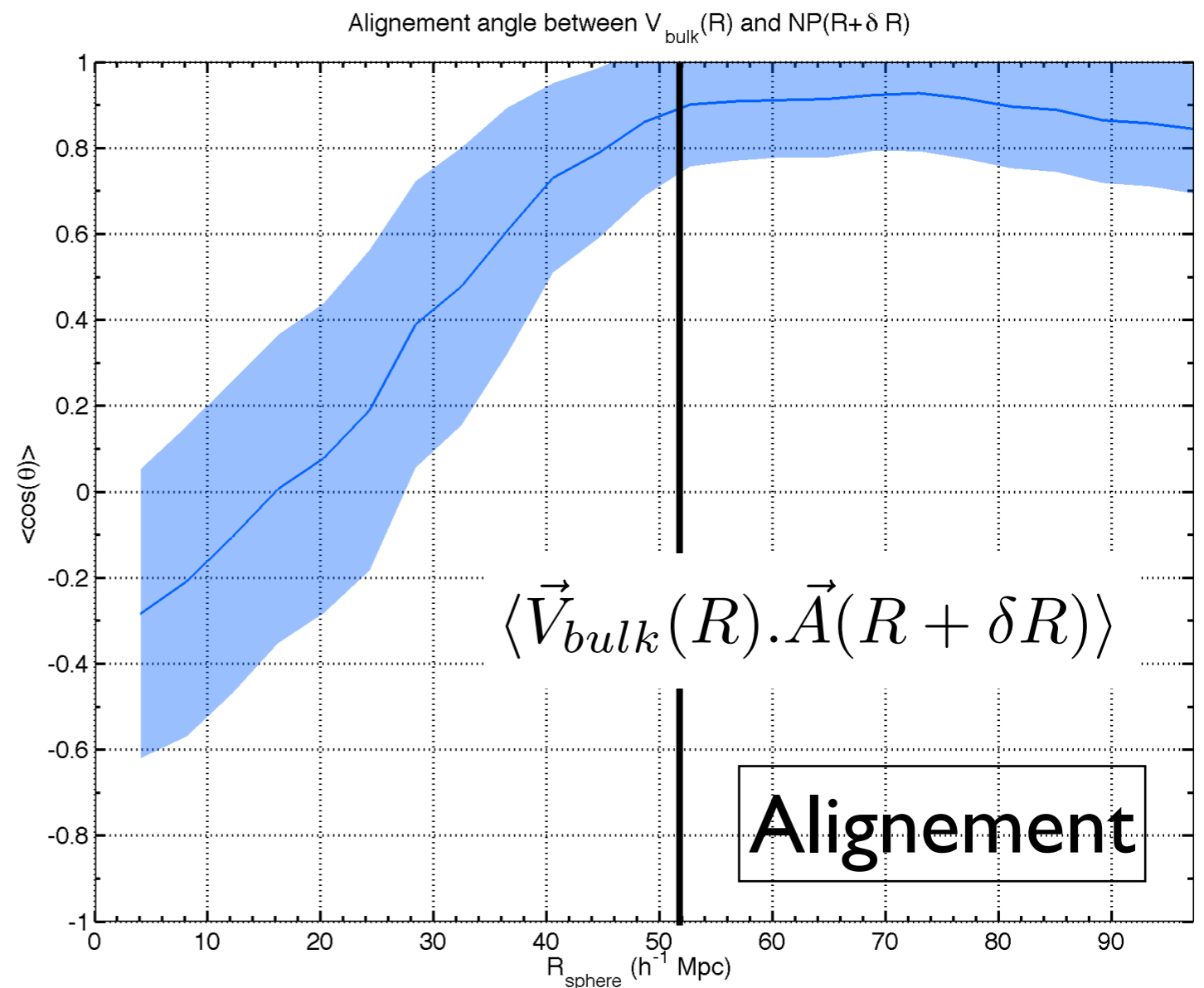
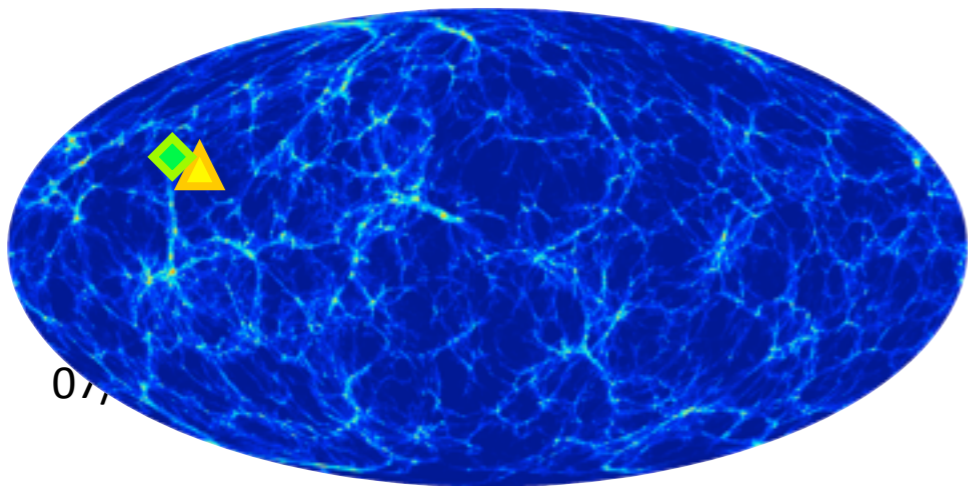
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A CHARACTERISTIC SCALE

- ❖ Asymmetry integrated in spheres:
 - ◆ Scalar product of the bulk flow vector at radius R with the asymmetry in spheres of larger radius $R+\delta R$.

- ❖ The mean shift δR between the velocity and the density fields is:

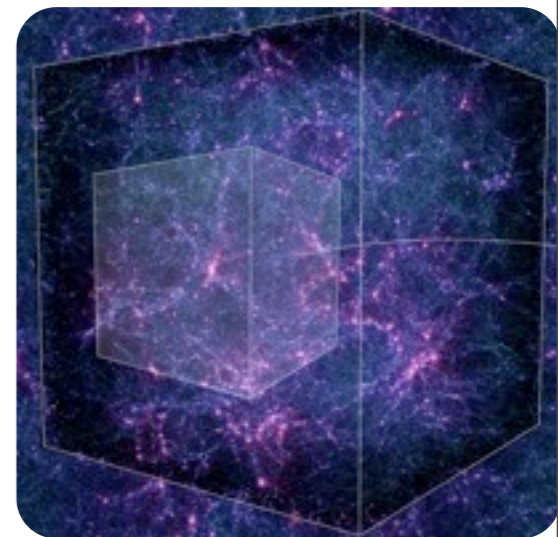
$$\delta R = 32 \pm 4.1 h^{-1} \text{ Mpc.}$$





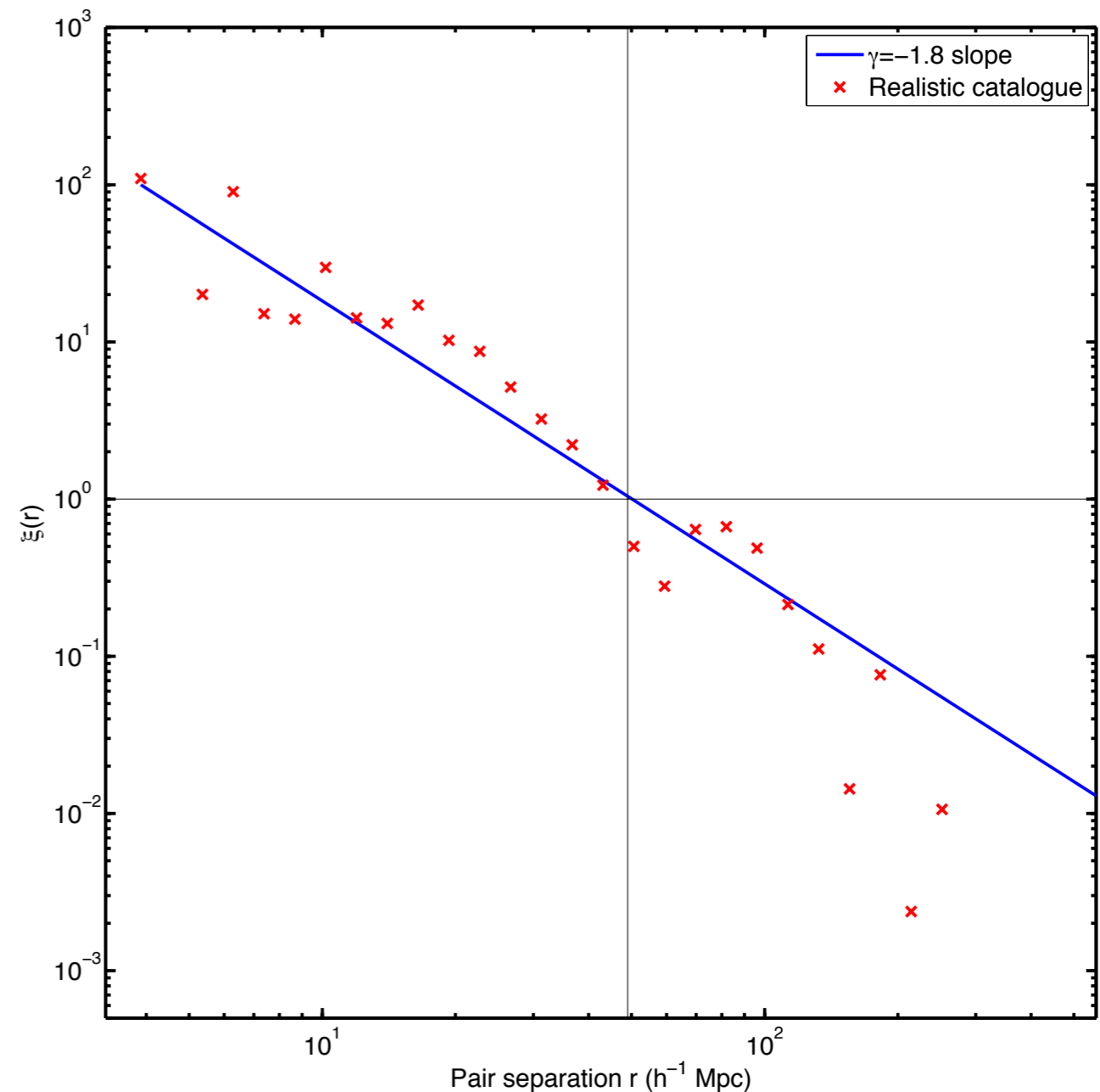
V.SPATIAL DISTRIBUTION OF HIGH VELOCITY COSMIC FLOWS

- 1) Origin of asymmetry
- 2) Density peak reconstruction
- 3) Distance to neighboring density peaks



ORIGIN OF ASYMMETRY

- ❖ The centers of the realistic catalog are not randomly distributed.
- ❖ What structures (voids, filaments, clusters...) can trigger such an asymmetry?
- ❖ Characterize neighbors density peaks.

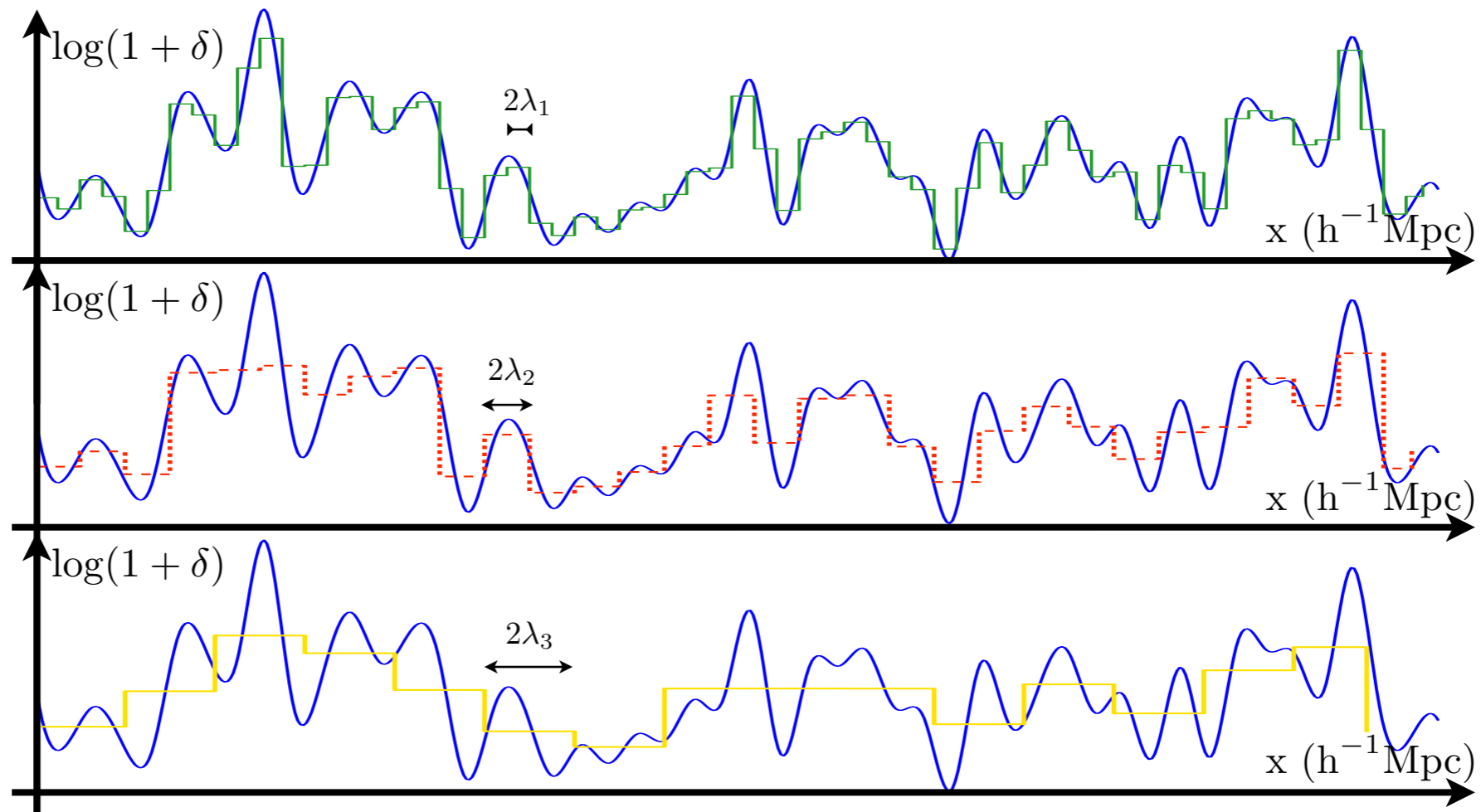


DENSITY PEAK RECONSTRUCTION

- ❖ Compute accurate density field from a set of particles using SPH smoothing:

$$\rho_i = \rho(\vec{r}_i) = m \sum_j W(|\vec{r}_i - \vec{r}_j|, \lambda)$$

- ❖ One free parameter: kernel λ .



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DISTANCE TO NEIGHBORING PEAKS

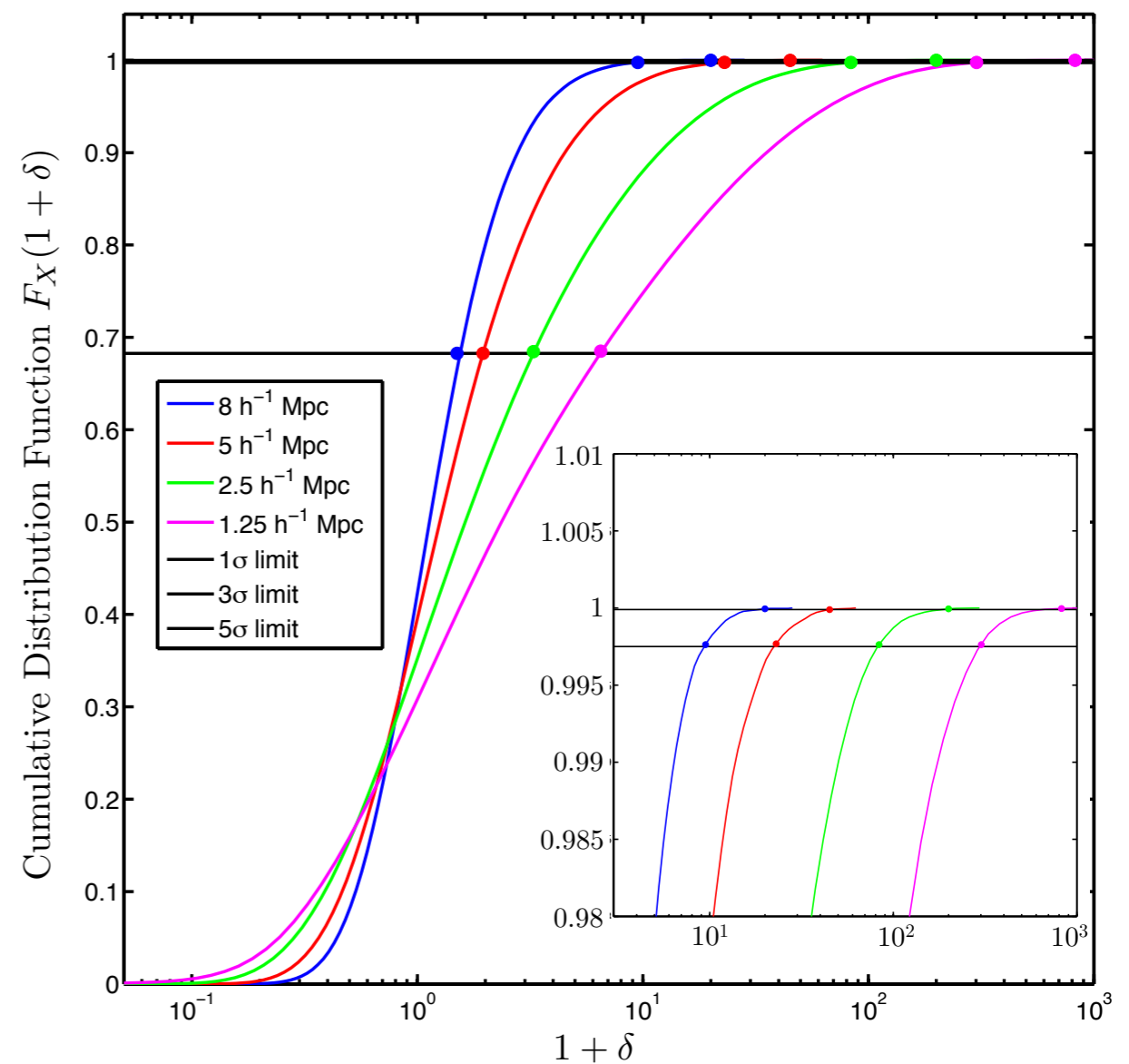
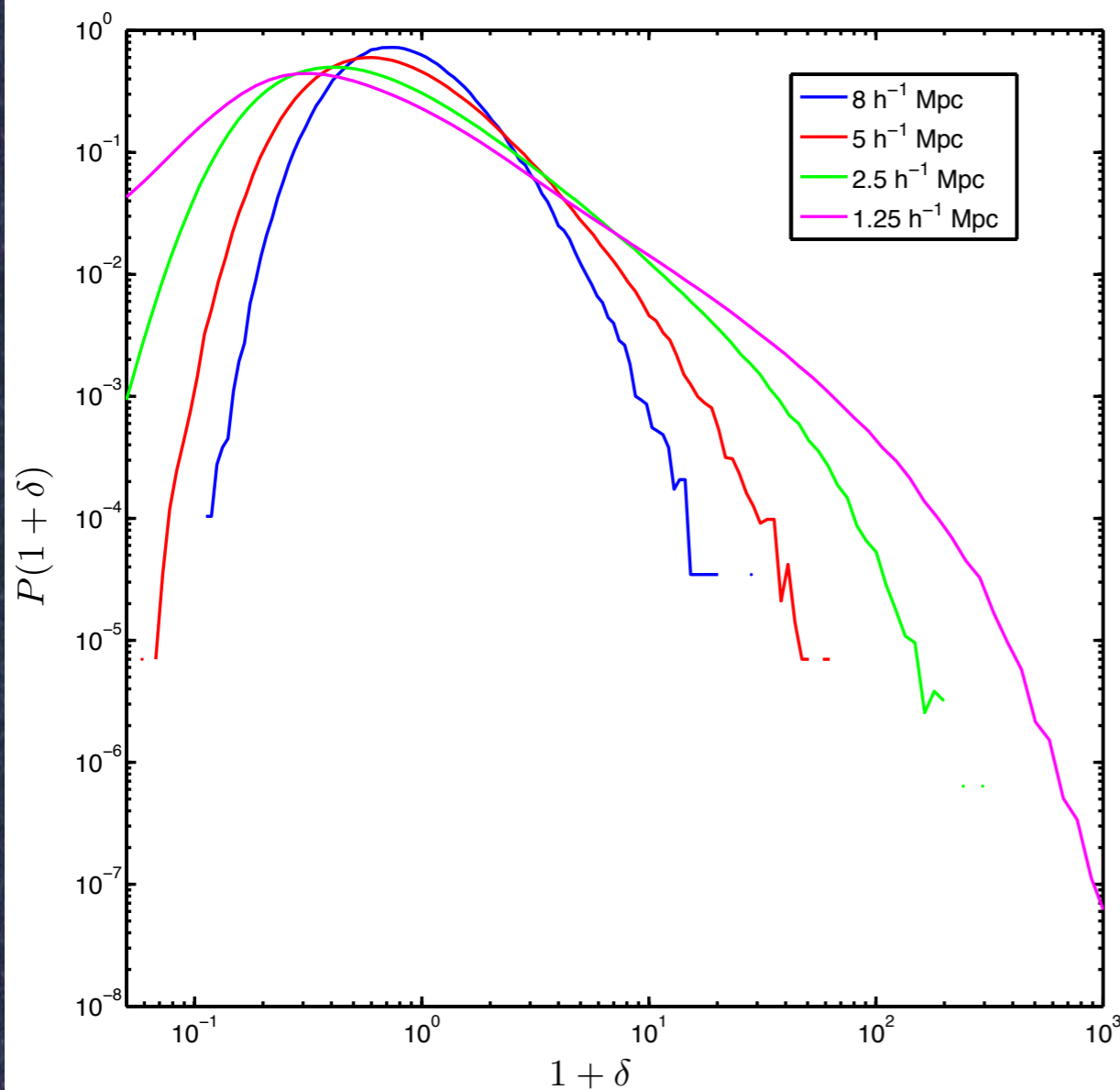
- ❖ The mean mass contained in a SPH bubble of mean density δ is:

$$\bar{M} = \frac{4}{3}\pi\lambda^3\bar{\rho}(1 + \delta)$$

- ❖ Compute separations between closest density peaks and centers of the realistic catalog:
 - ◆ Clear definition of centers of the realistic catalog.
 - ◆ What closest density peaks?
- ❖ Second free parameter: peak height threshold Δ .
- ❖ Remaining issue: determine the (λ, Δ) parameters.

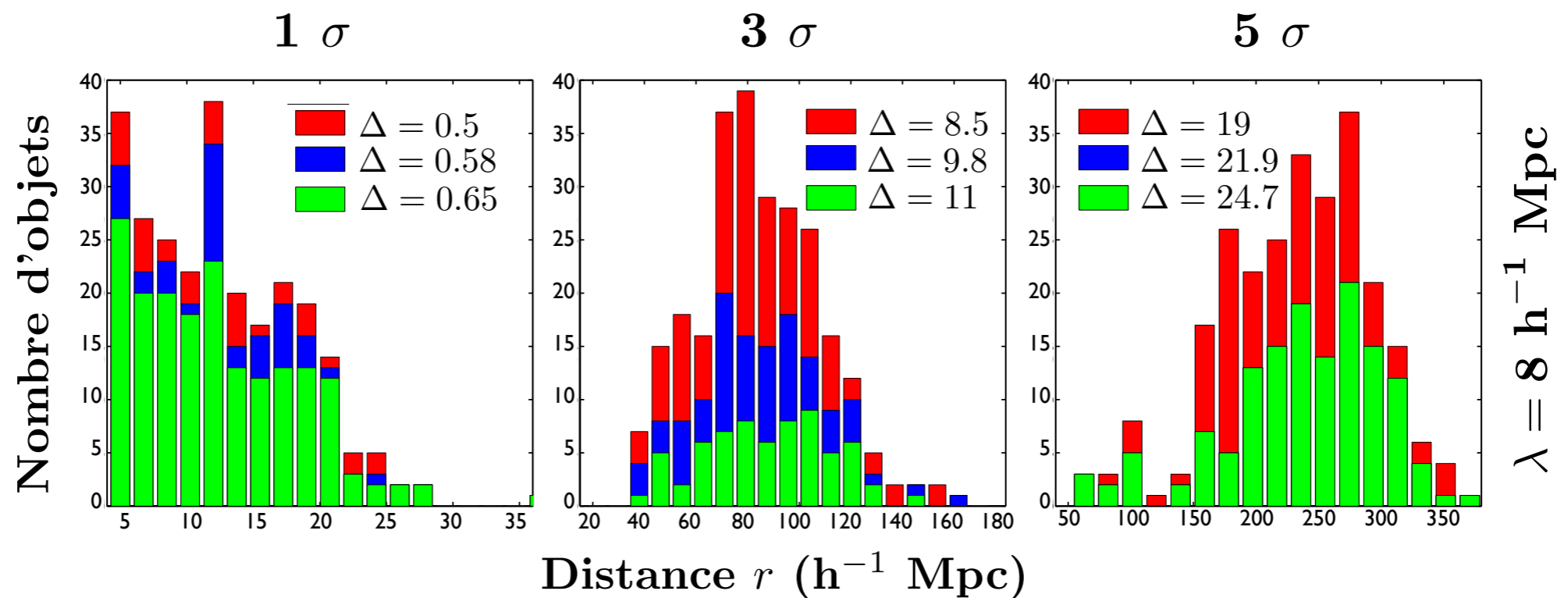
DISTANCE TO NEIGHBORING PEAKS

- ❖ A univocal way to set the free parameters (λ, Δ) :
 - ◆ Statistical criterion on the cdf of overdensities: 1σ , 3σ , 5σ confidence levels.



DISTANCE TO NEIGHBORING PEAKS

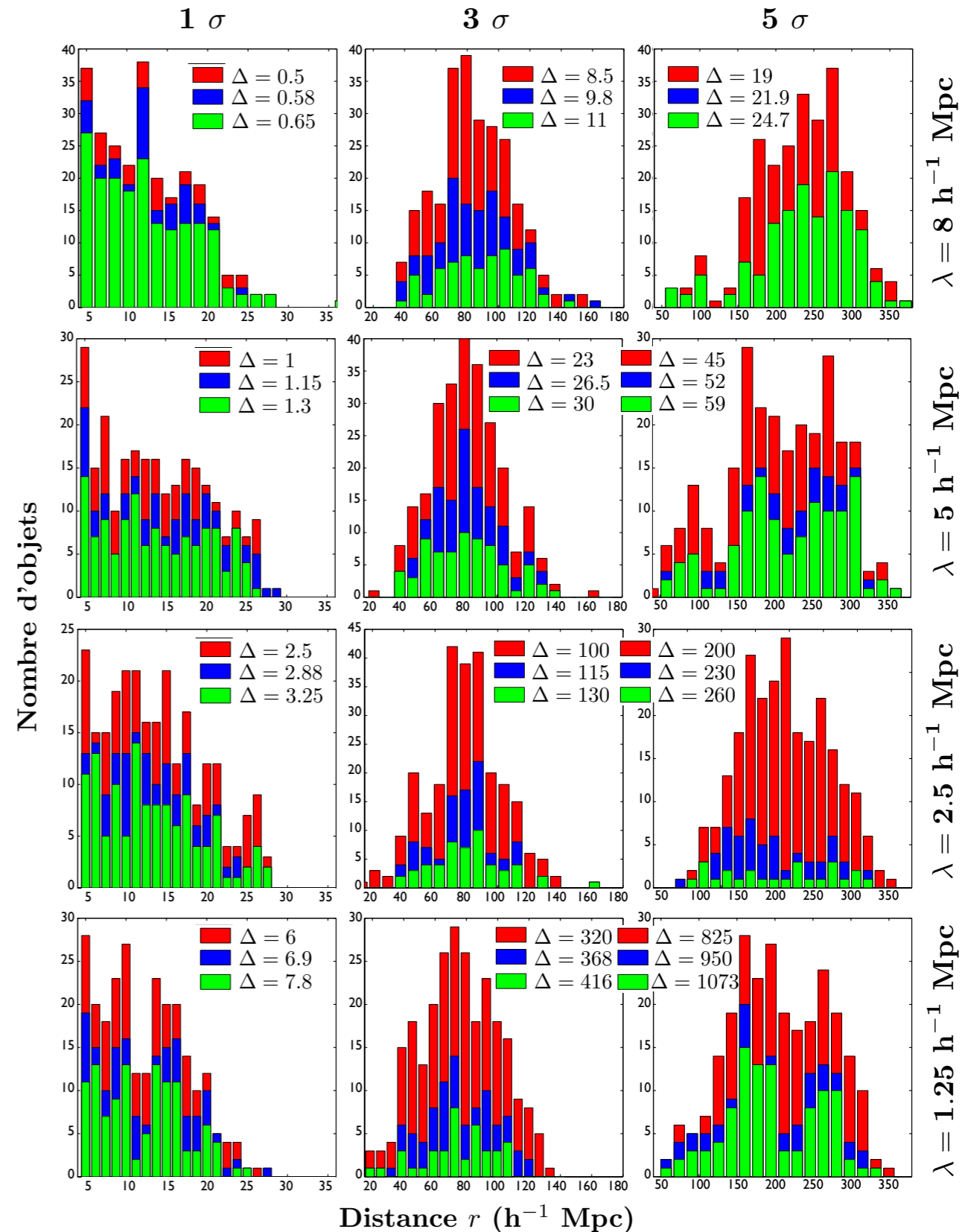
- ❖ Histogram of the distance between an observer with high velocity cosmic flows and a density peak smoothed at radius λ and above threshold Δ .
- ❖ Colors indicate various thresholds based on the σ one.



DISTANCE TO NEIGHBORING PEAKS

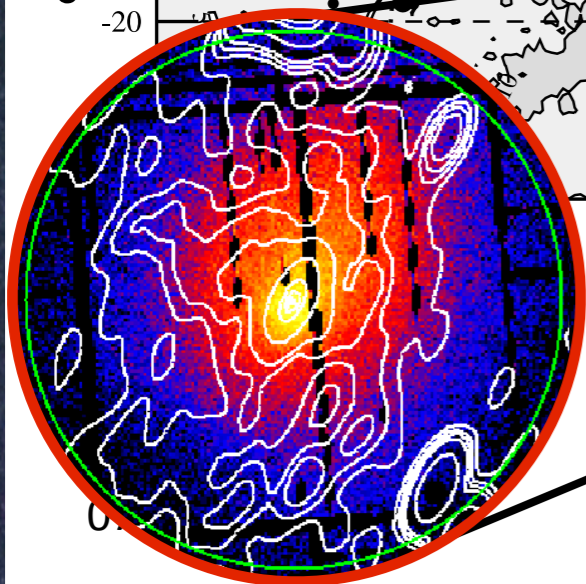
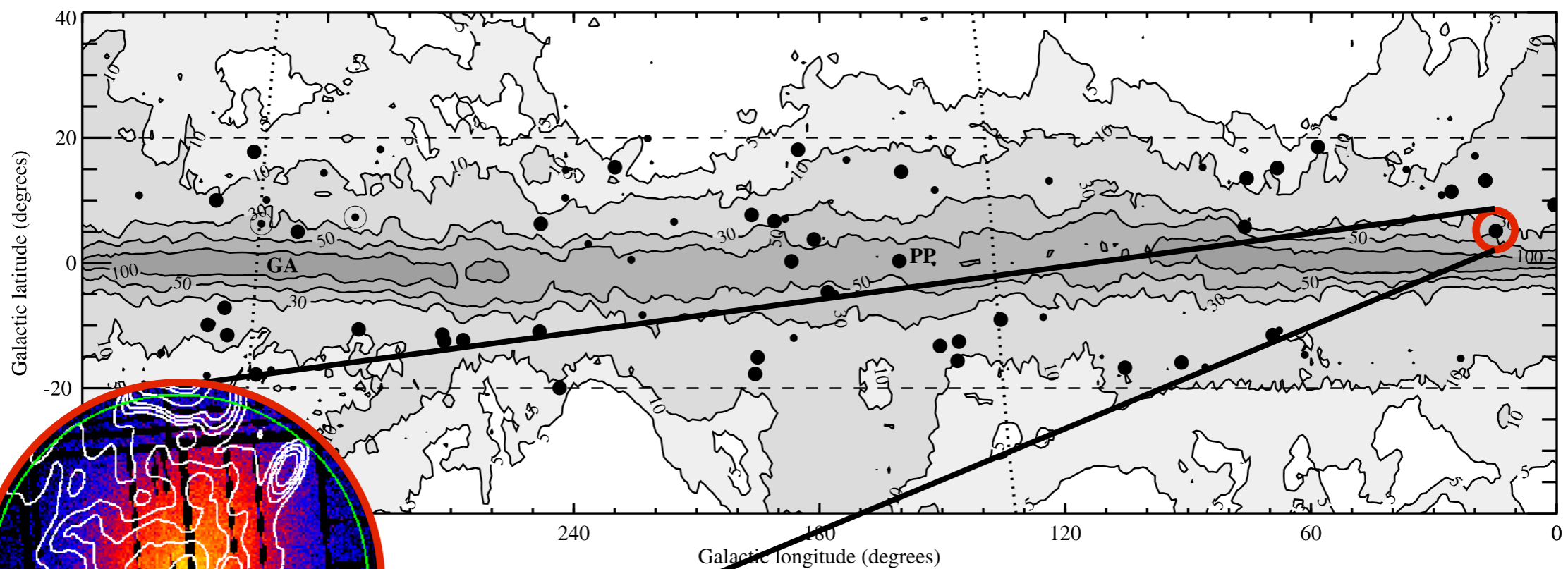
- ❖ Variation with the kernel:
 - ◆ 1 σ density peaks: plateau + quick decrease.
 - ◆ 3 σ density peaks: gaussian (similar moments).
 - ◆ 5 σ density peaks: depends on the kernel.
- ❖ Whatever λ , peak height at 3 σ gives $M=7.10^{14} h^{-1} M_{\odot}$ at 80 h^{-1} Mpc.

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DISTANCE TO NEIGHBORING PEAKS

- ❖ A cluster candidate in the Zone of Avoidance (Ebeling et al. 2002, Kocevski et al. 2005)
- ❖ Ophiuchus cluster, mass $5.10^{14} h^{-1} M_{\odot}$, at $80 h^{-1}$ Mpc.



Imprints of Dark Energy on structure formation



CONCLUSION

- ❖ Observations of a high velocity bulk flow at intermediate scales are due to a statistically rare event.
- ❖ The reconvergence of the bulk flow towards the linear amplitude at large scales is an new original cosmological probe.
- ❖ The dynamical origin of a high velocity bulk flow is linked with the asymmetry of the three-dimensional matter field at higher scales ($\sim 85 h^{-1}$ Mpc).
- ❖ Those observers are occupying particular over-dense places at $\sim 80 h^{-1}$ Mpc from a high density peak.



CONCLUSION

- ❖ This presentation: cosmological velocity fields.
- ❖ Density field can give information on different aspects:
 - ◆ Power spectra.
 - ◆ Correlation functions and Haloes-Dark-Matter biases.
 - ◆ Mass functions in redshift and comoving space.
 - ◆ Covariant perturbations theory in general multi-fluids cosmology.

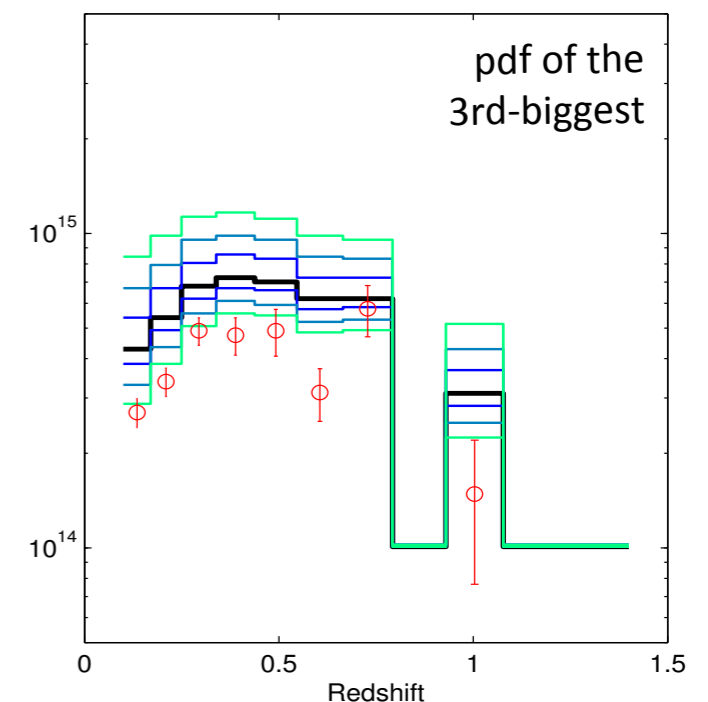
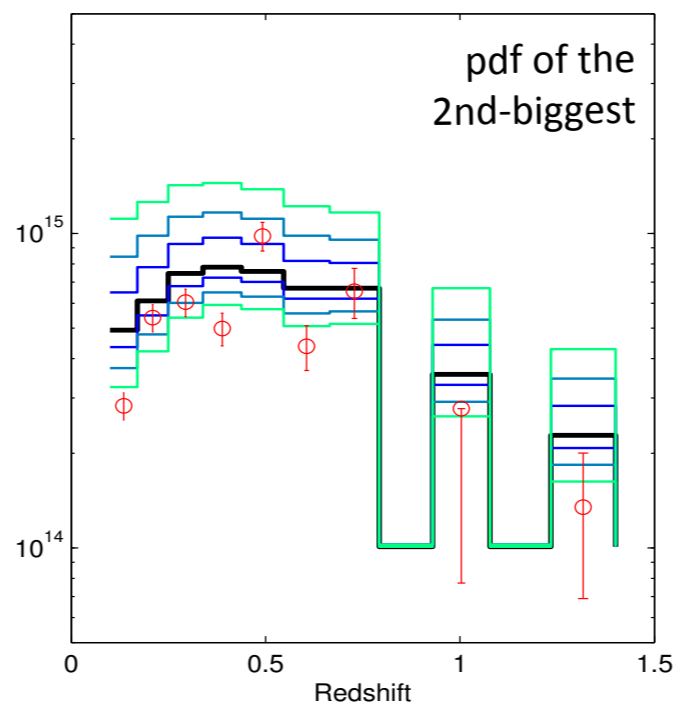
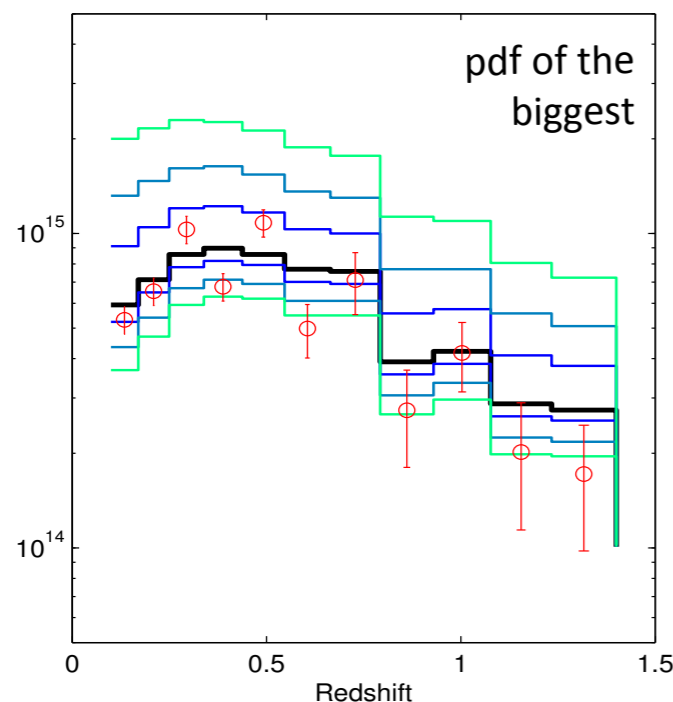


CONCLUSION

- ❖ Importance of efficiency to get new simulations to tackle new scientific problems:
 - ◆ Optimization of the communication scheme (BlueGene vs Bullx) of the RAMSES dynamical code.
 - ◆ Various optimization of the pFoF halo finder code.
- ❖ Fast correlation function computation methods.
- ❖ Population of Dark Matter haloes with galaxies (e.g. Markov chains).

CONCLUSION

- ❖ How can we populate Dark Matter haloes from HOD?
- ❖ Extreme value statistics:
 - ◆ What is the distribution of the most massive Dark Matter haloes at a given redshift in a given cosmology?
 - ◆ What is the distribution of the mass of the k th-biggest Dark Matter haloes at a given redshift in observations?

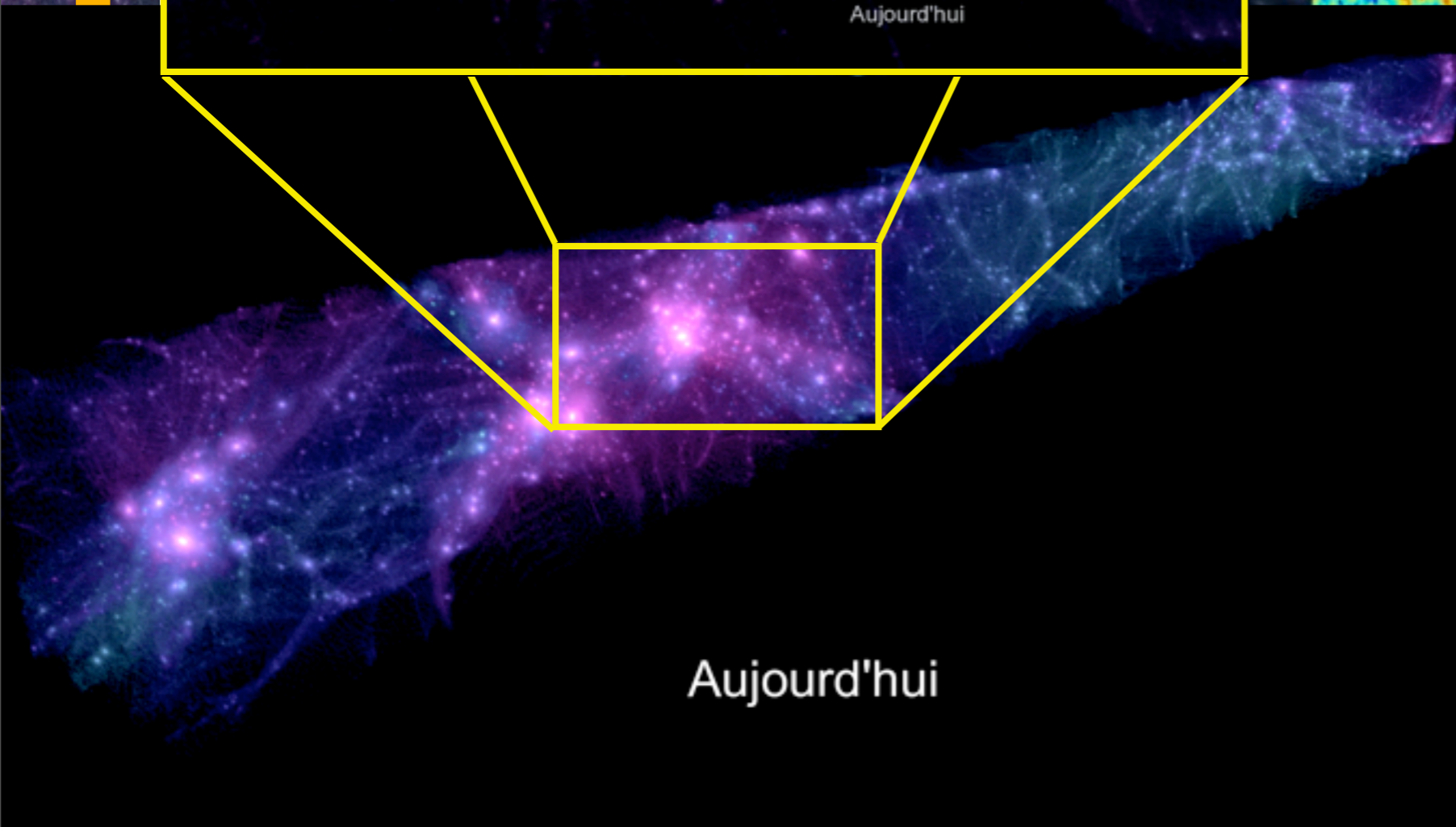




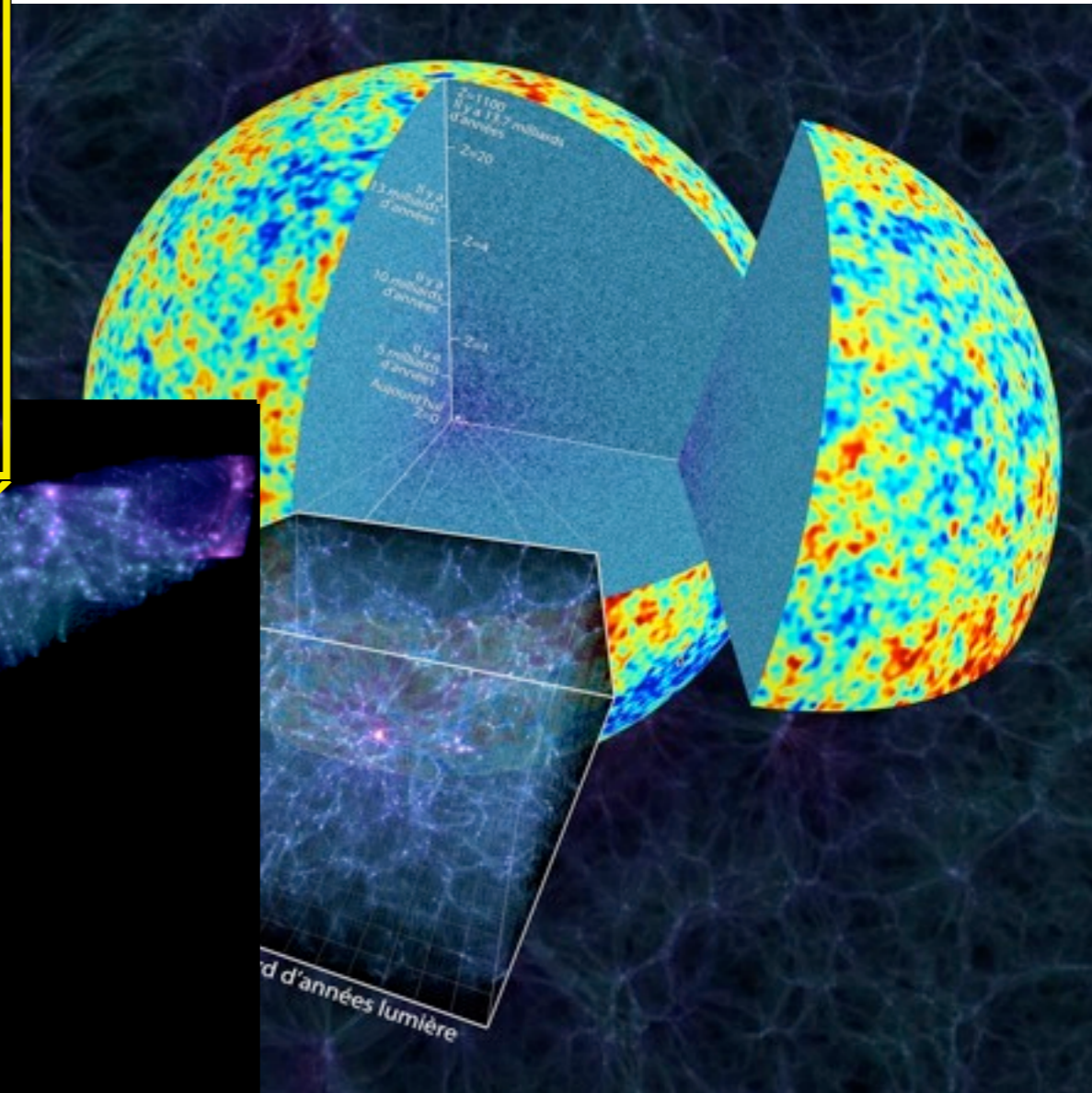
QUESTIONS & COMMENTS !



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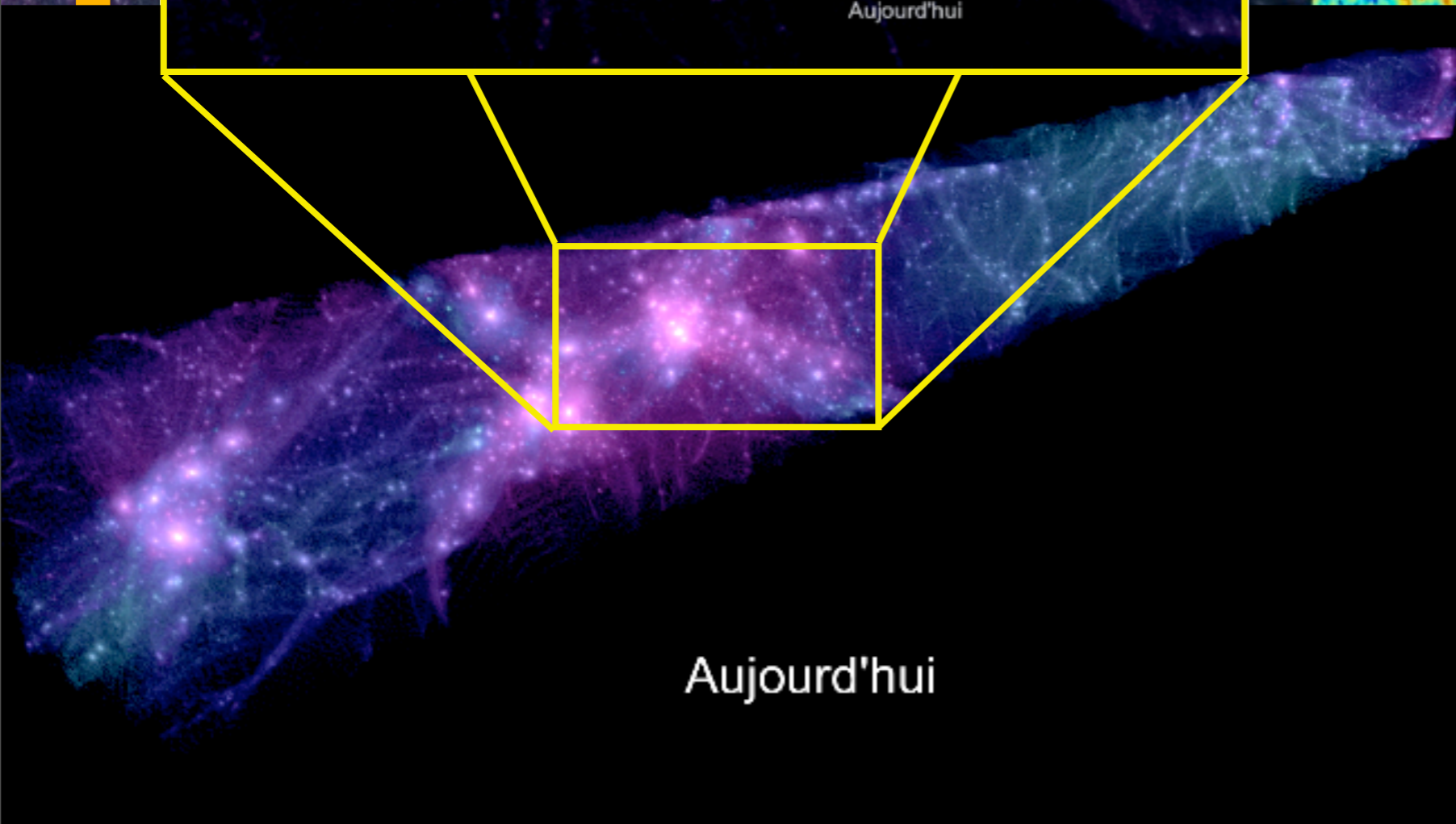
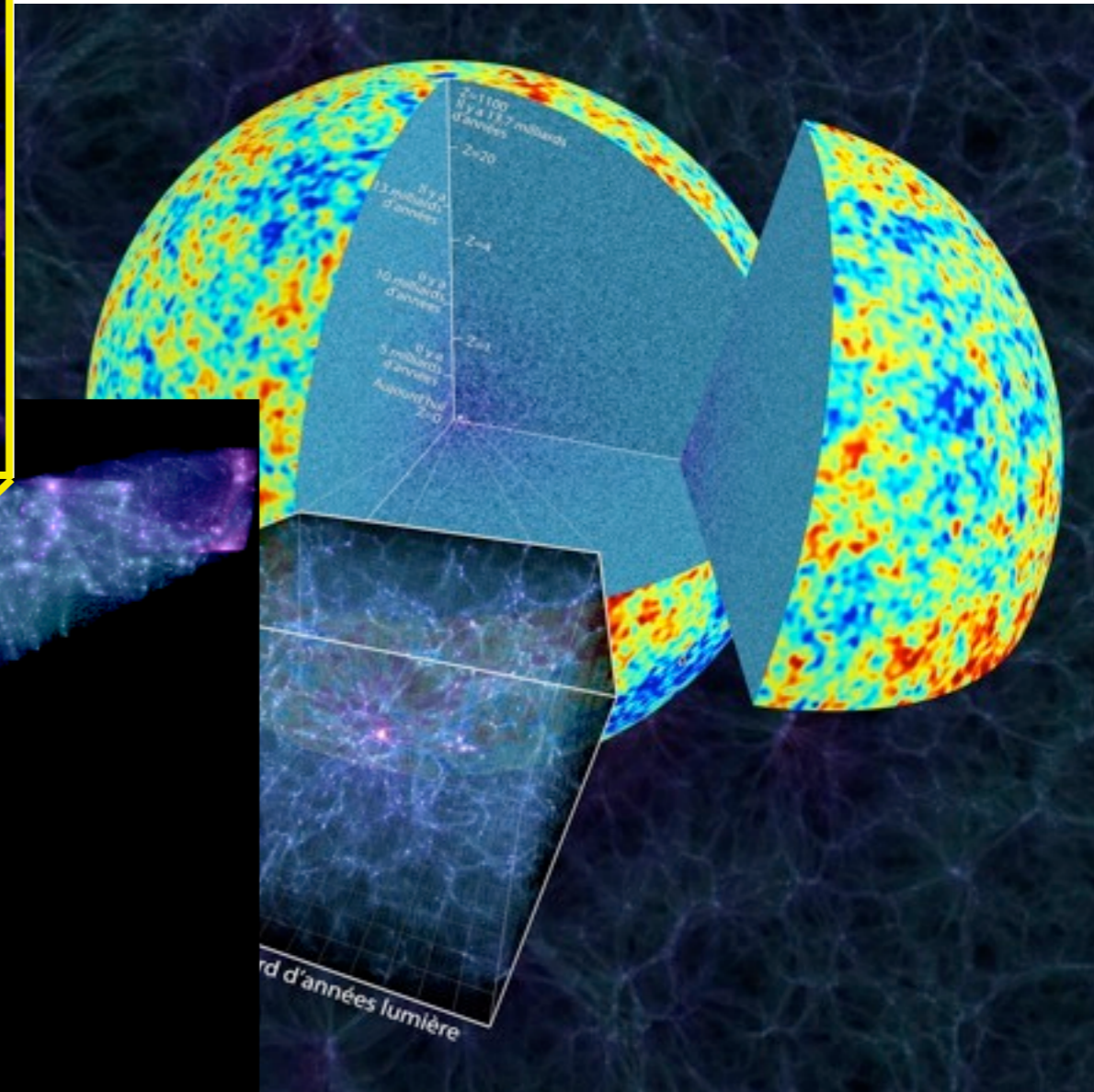
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QUESTIONS & COMMENTS !

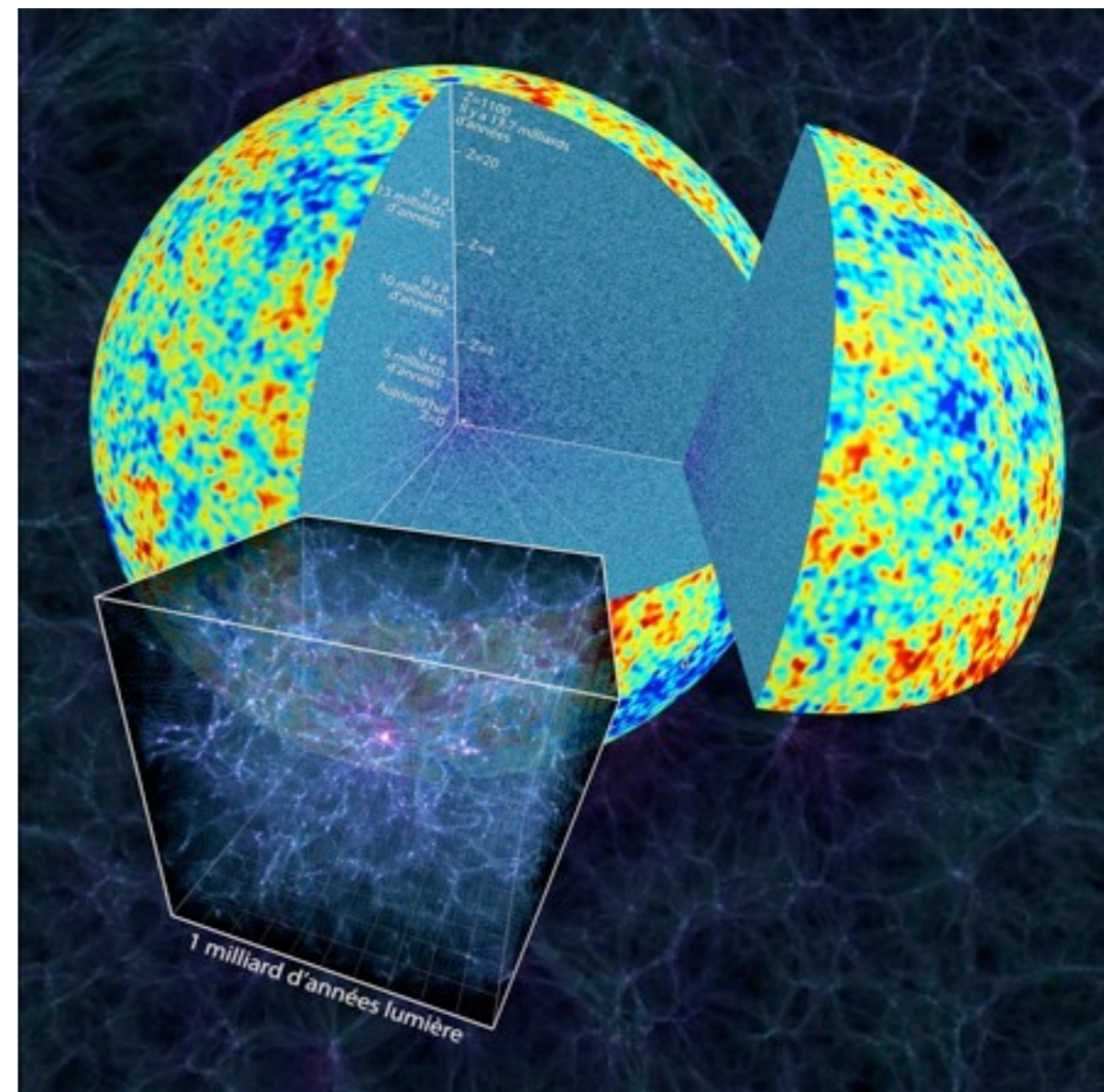
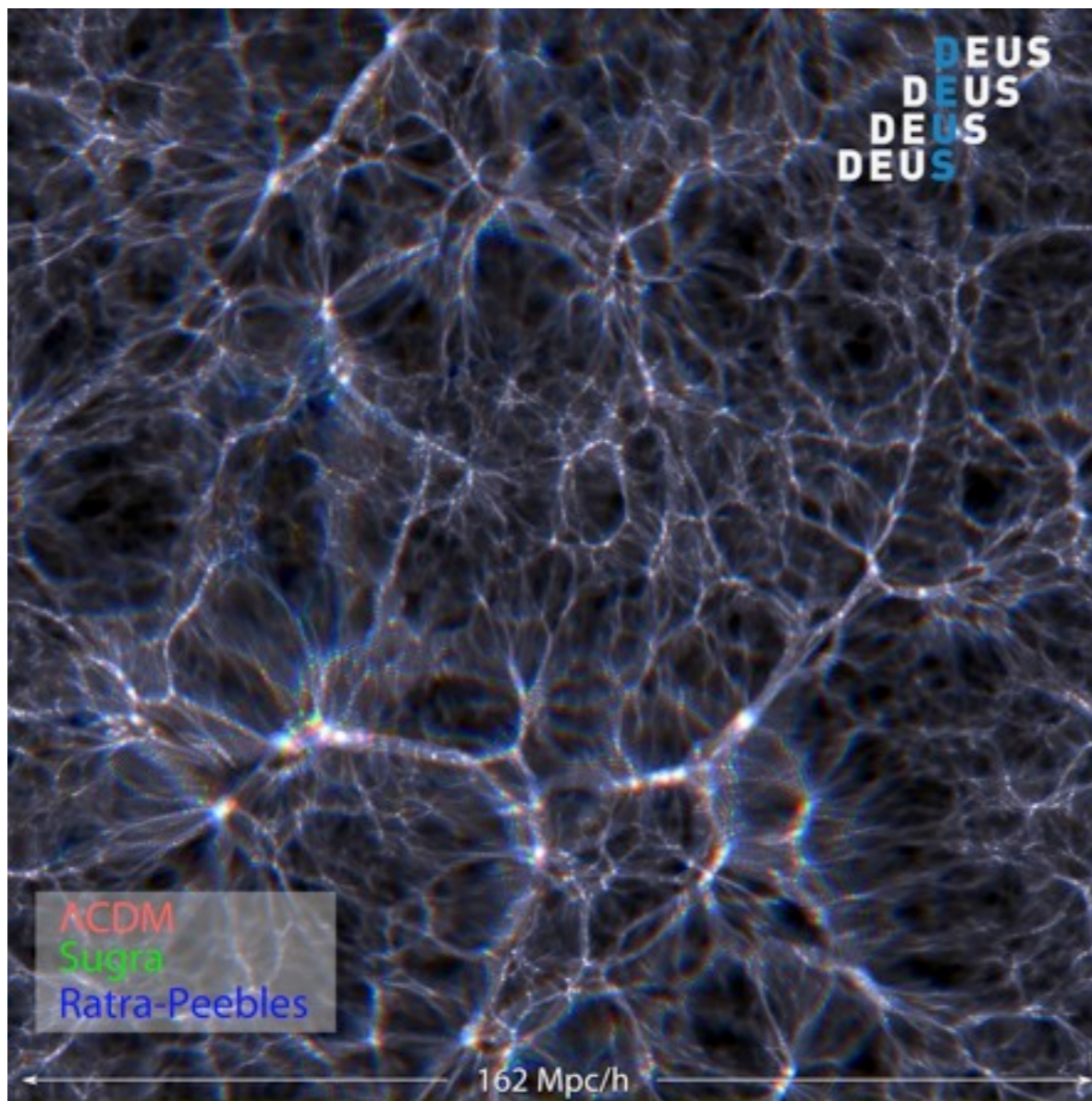


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QUESTIONS & COMMENTS !





TOOLBOX

❖ Toolbox:

- ◆ Malquist bias - In brightness-limited survey
The average measured lum. of a survey will be higher than the true one since only the brightest object can be seen at large distance.
- ◆ Octree structure at the right
- ◆ Ophiuchus: Détecté par le survey CIZA de Ebeling et Kocevski (2002-2005-2007).

